

# Workshop 2

- Examples from metaD and TPS
- Details of the *shooting* approach
- Details of MD engines

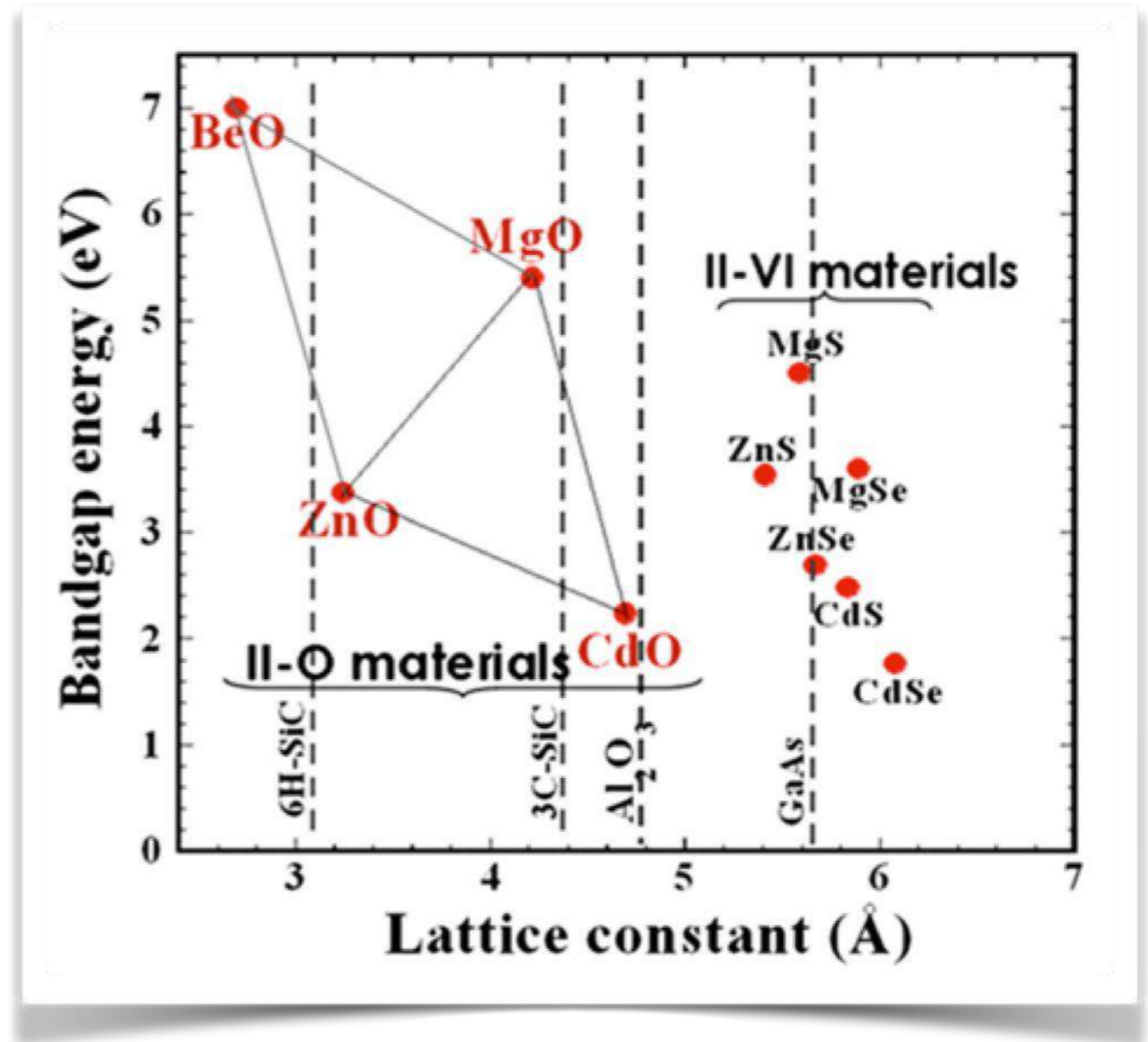
# Metashooting

- combine metaD and TPS
- based on an external driver
- cp2k/plumed/shooter

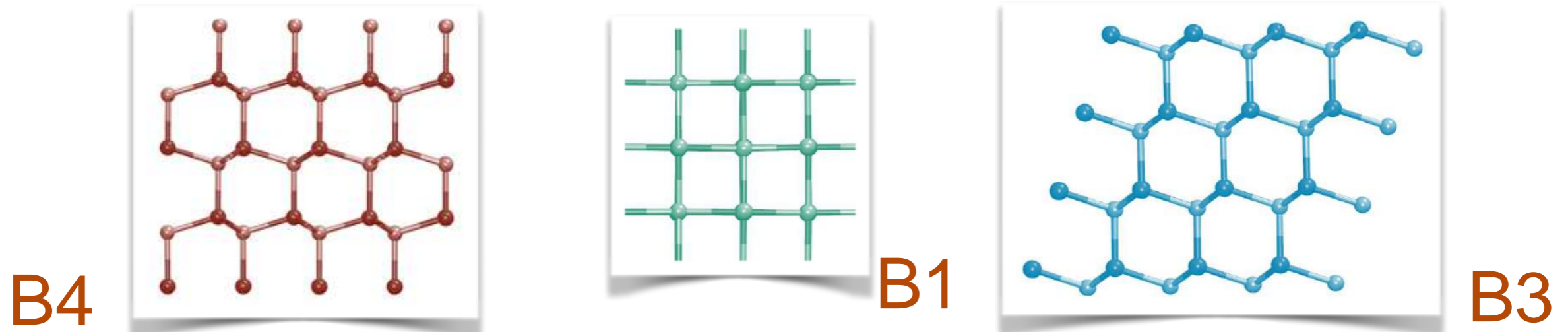
# ZnO

Binary oxide, small lattice constant (d shell)

Wurtzite normal state, zincblende metastable, transformation to B1 (rocksalt) under pressure



# Zinc Oxide (ZnO)



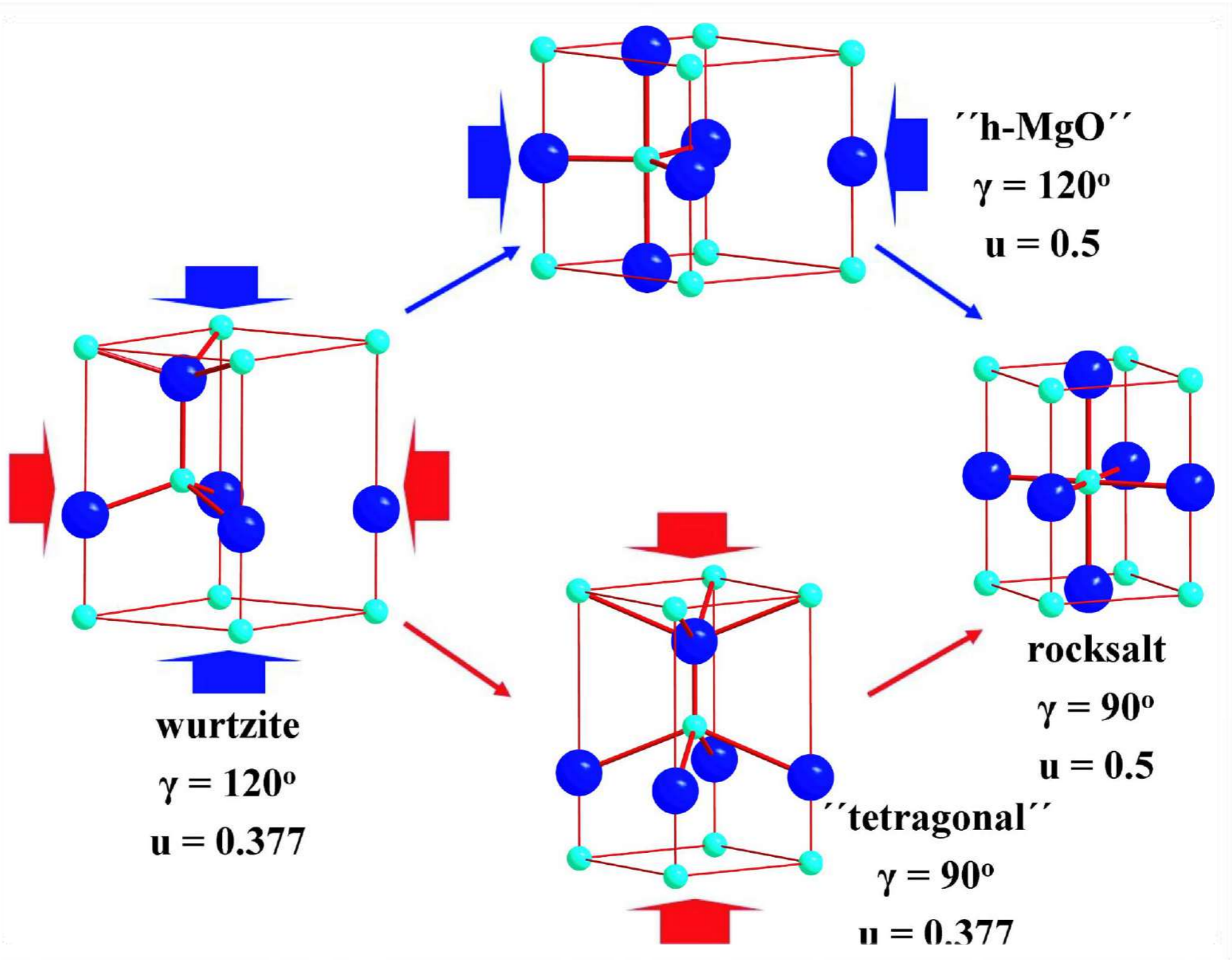
Hexagonal **wurtzite** (WZ, B4,  $P6_3mc$ ) structure under ambient conditions

High pressure **rocksalt** (RS, B1,  $Fm\bar{3}m$ ) accessible under extreme conditions

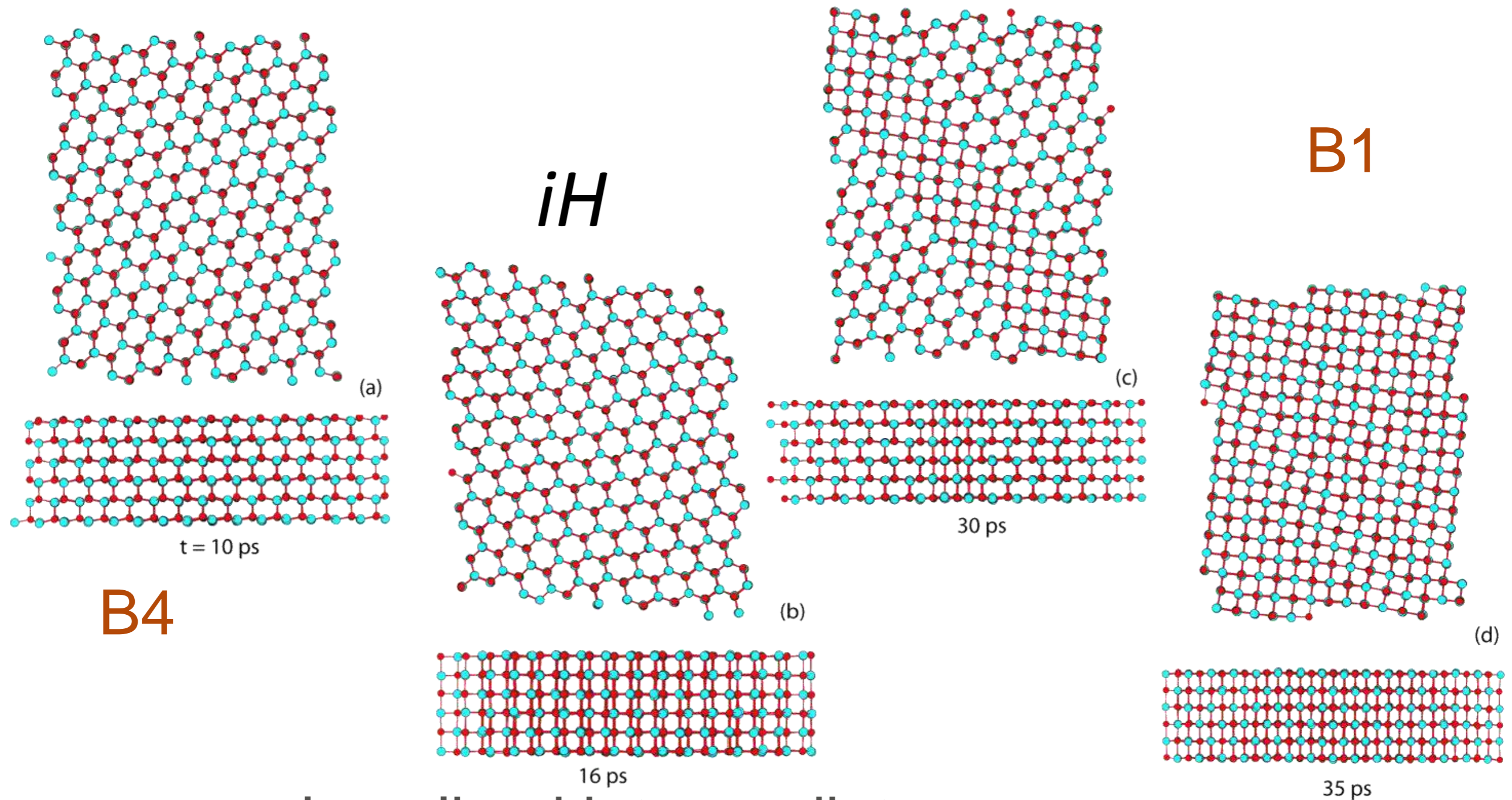
Cubic **zincblende** (ZB, B3,  $F43m$ ), also known as sphalerite, is metastable

# Intermediate Competition

GaN  
ZnO

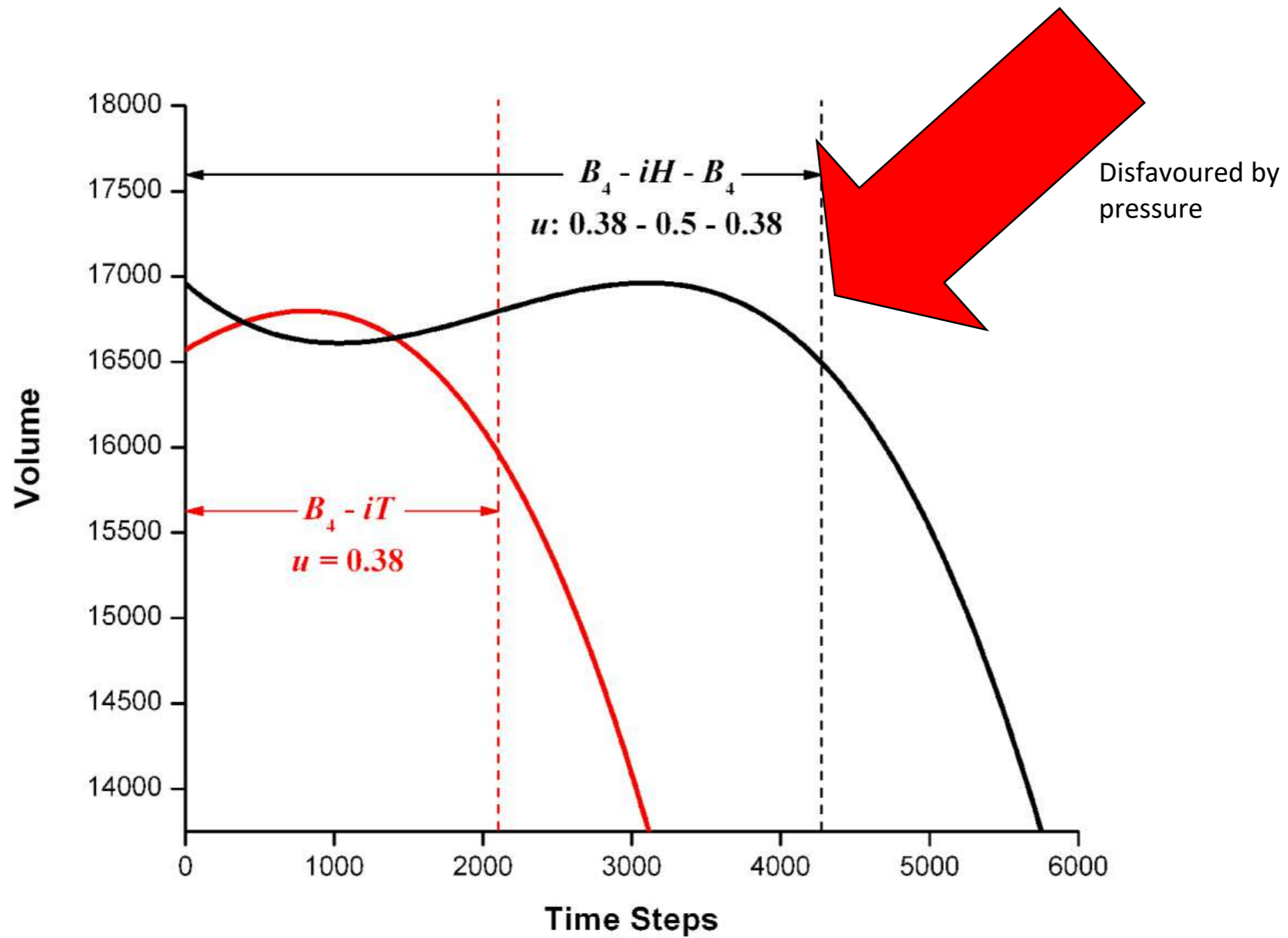


# ZnO: Competing Intermediates

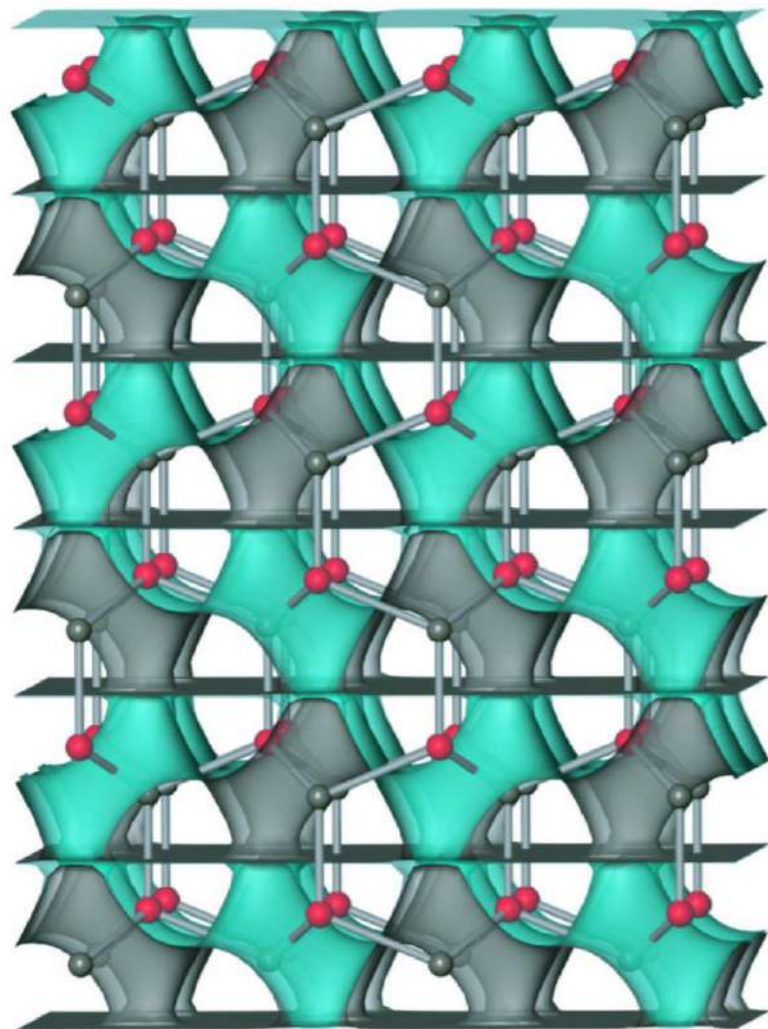


long lived intermediate

# Effect/role of pressure

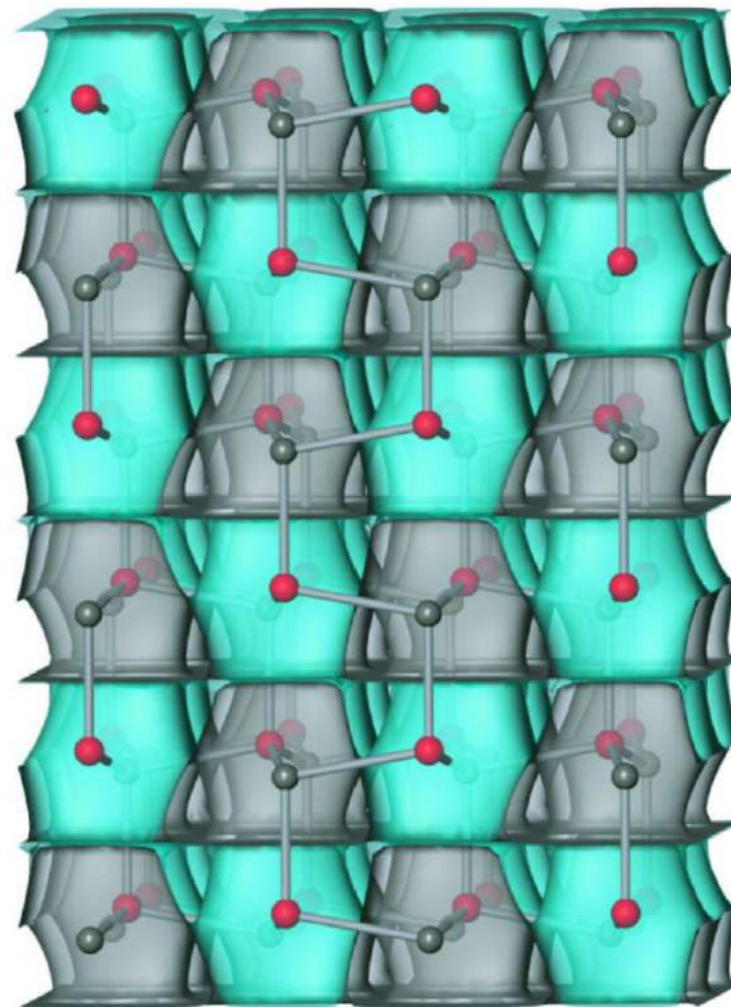


# B4 to B1 Phase Transition

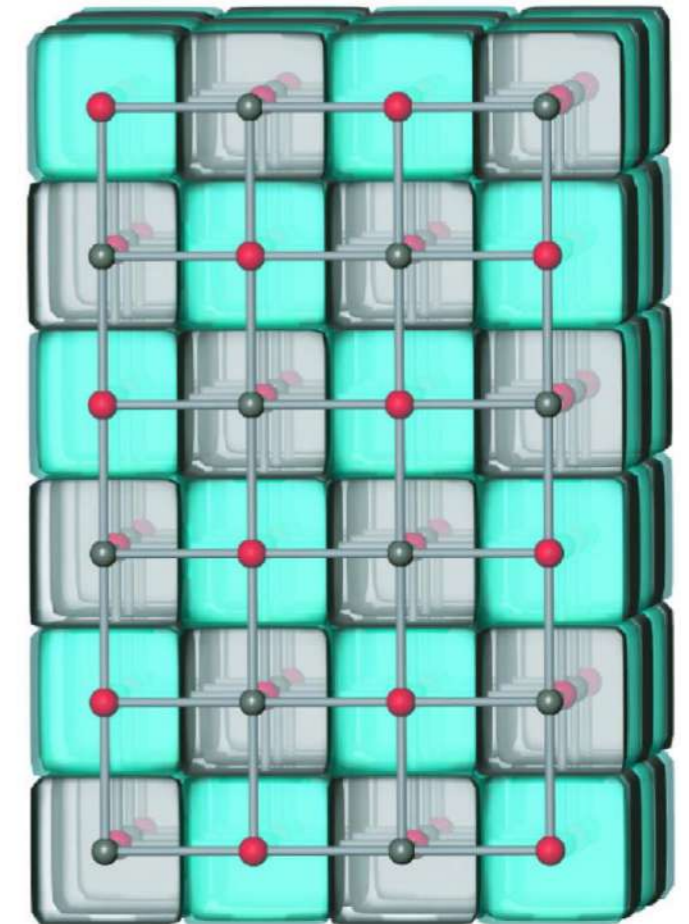


(wurtzite)

**B4**



Topological Intermediate

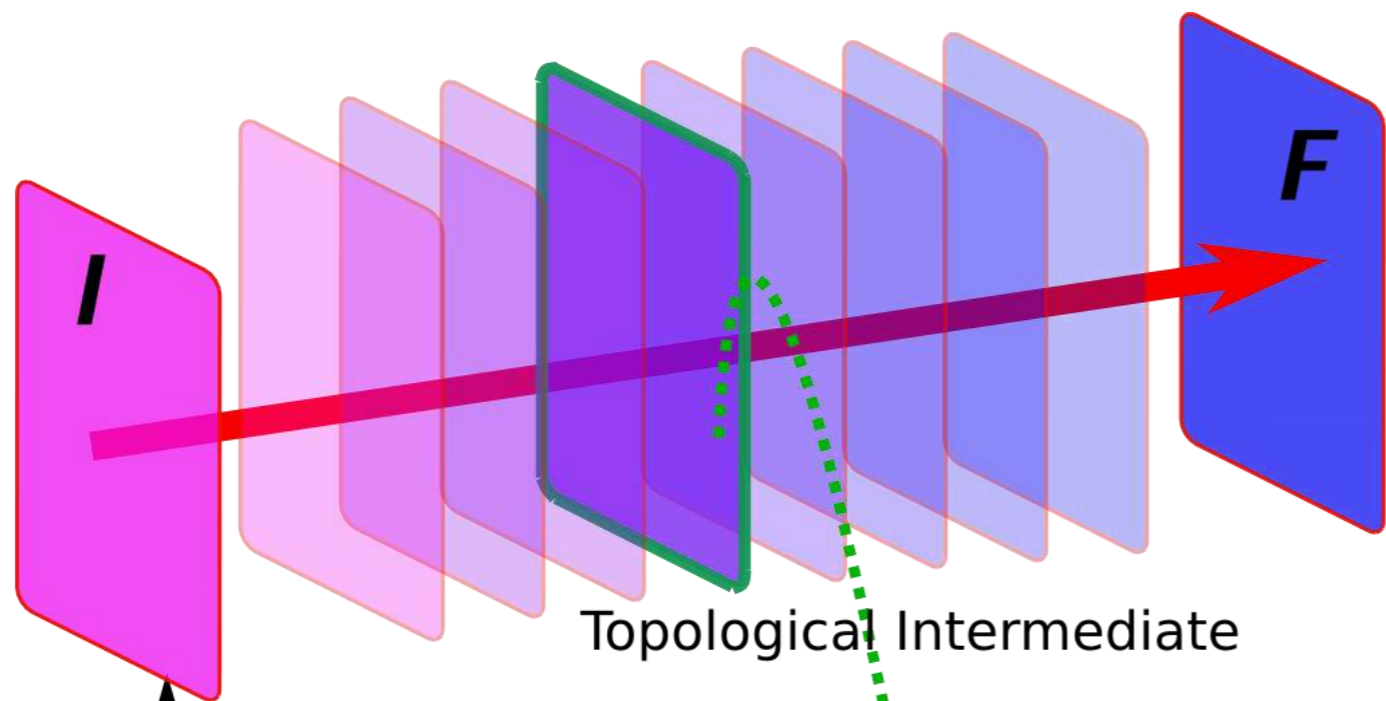


(rocksalt)

**B1**



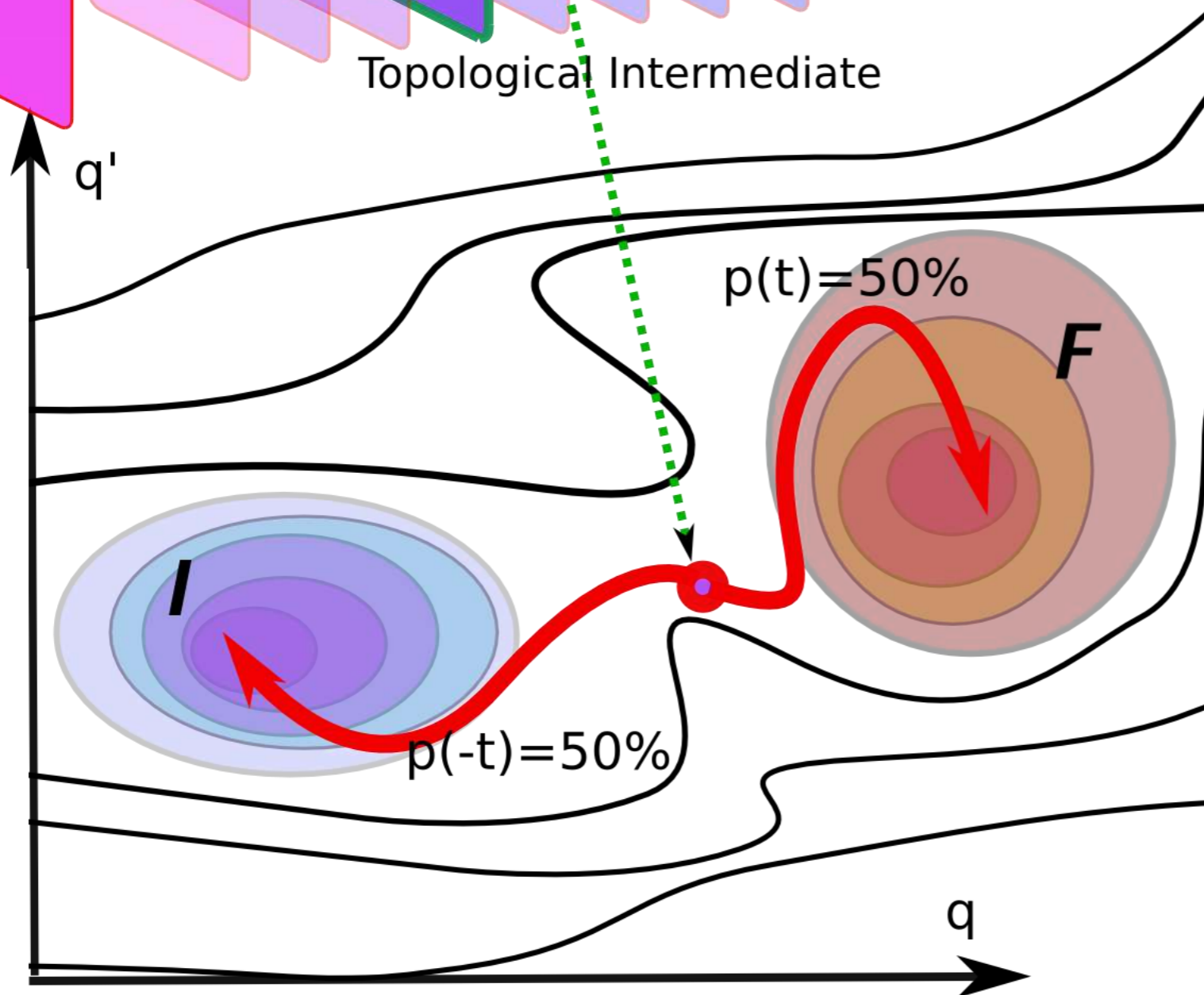




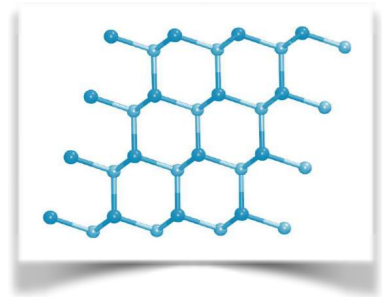
# Topology



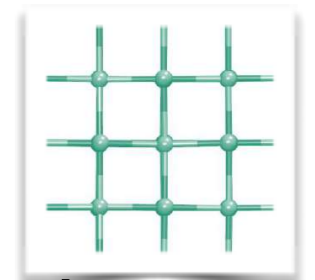
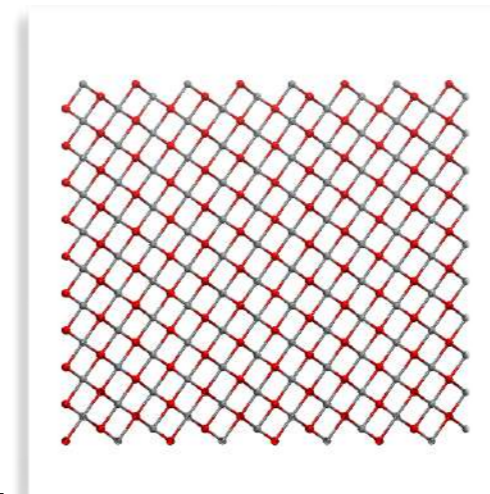
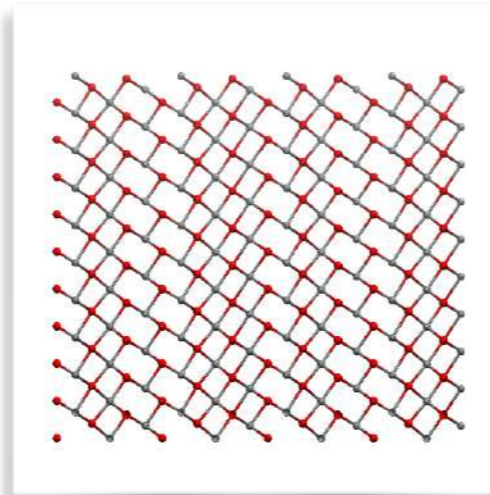
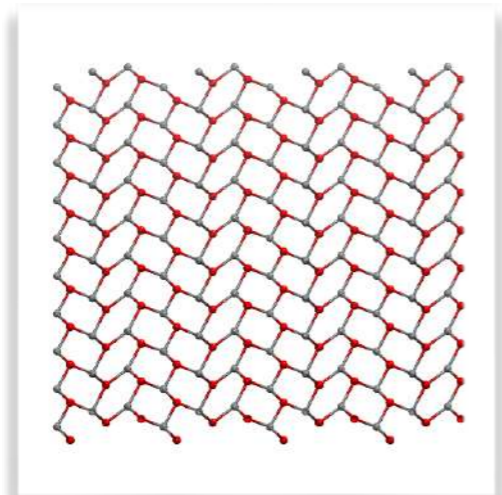
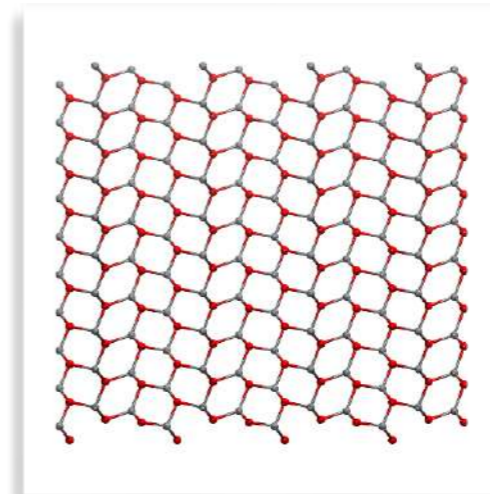
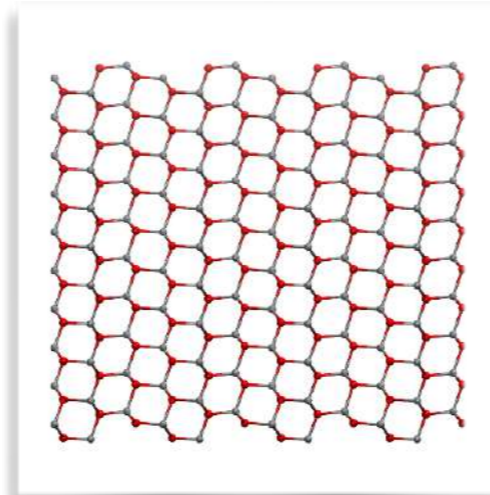
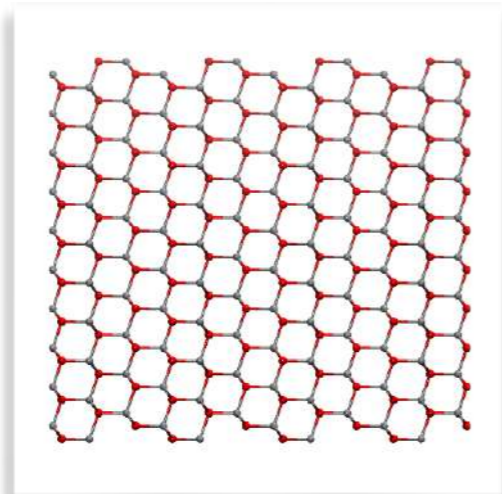
# MD



# First Trajectory

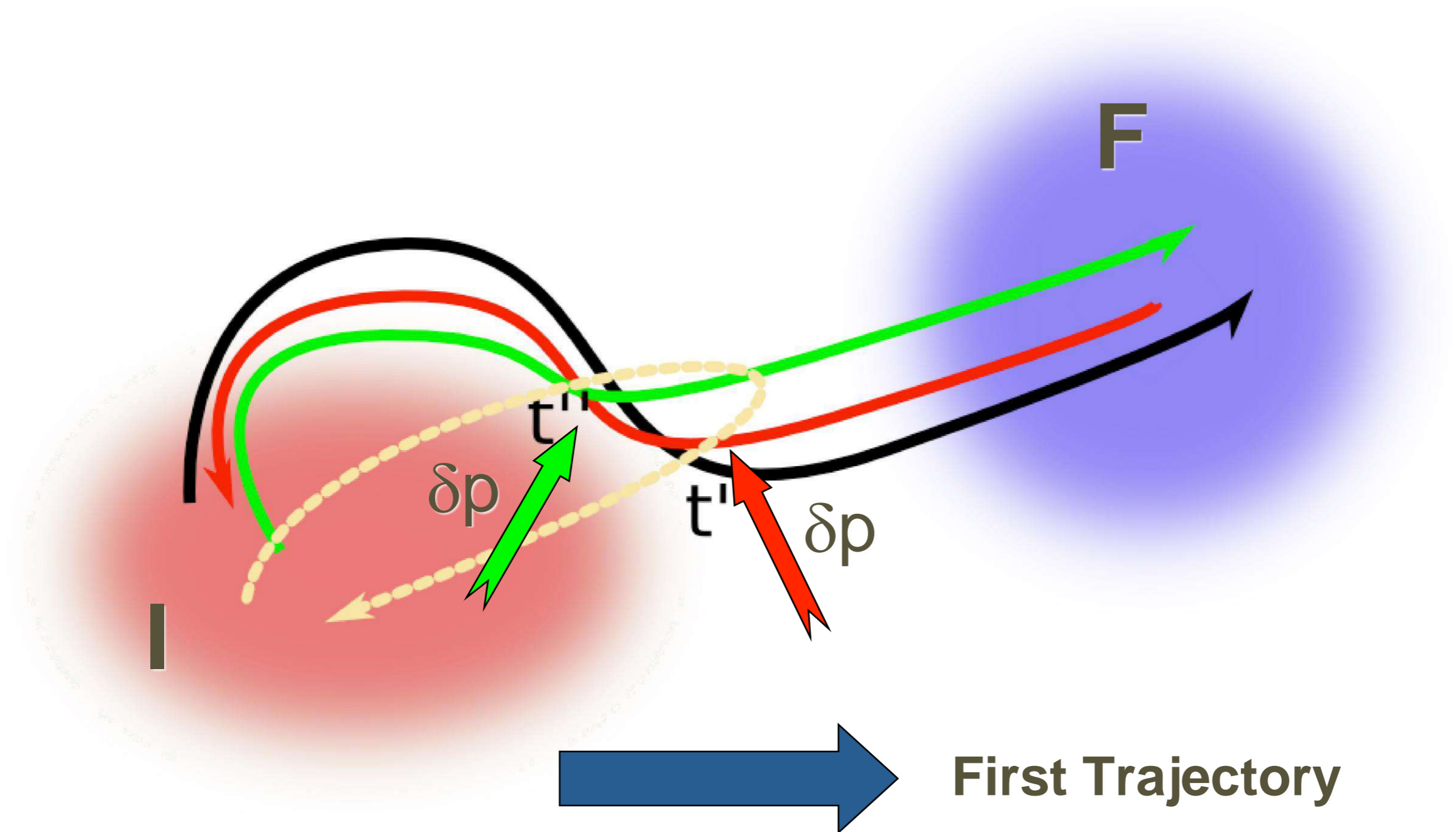


B3



A given trajectory does not need to be representative of the REAL transformation mechanism (TPS will weight its importance) **B1**

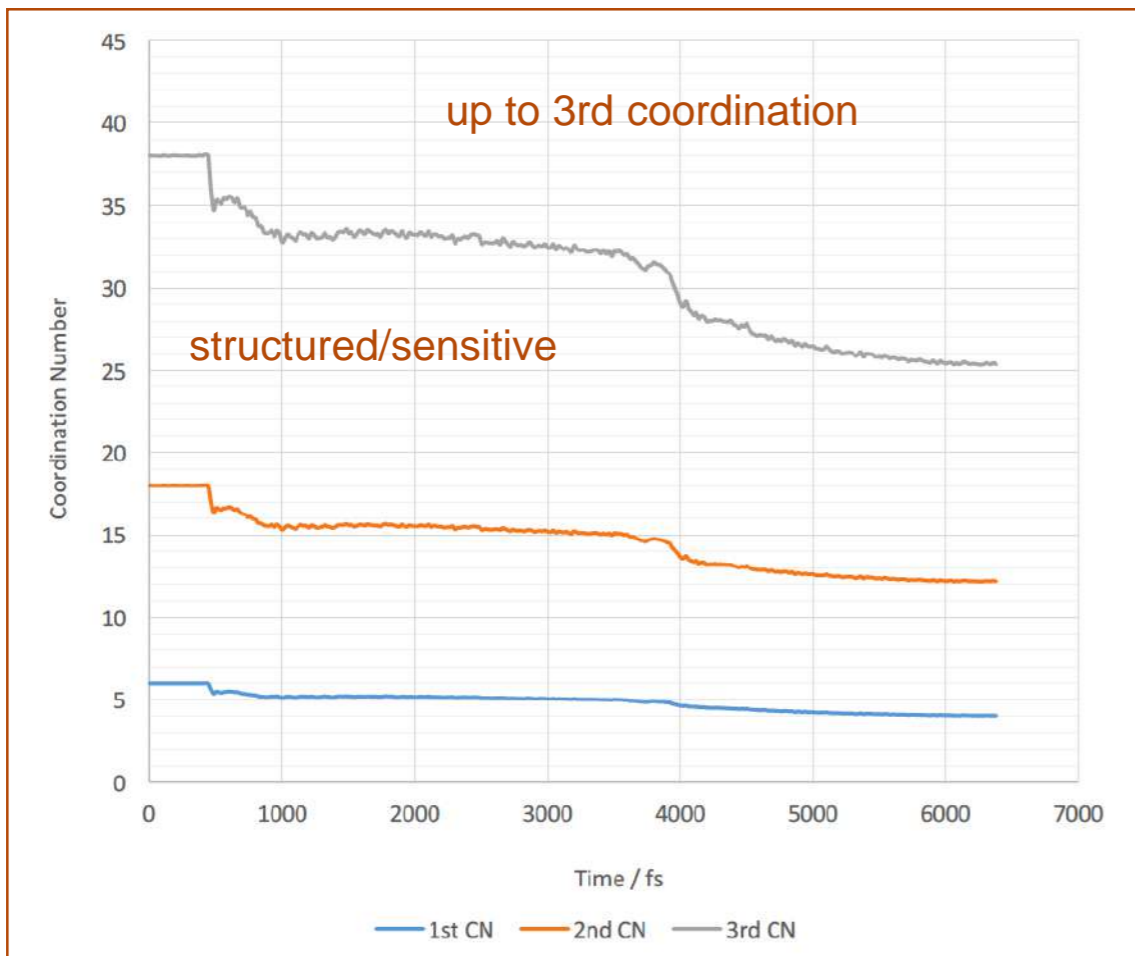
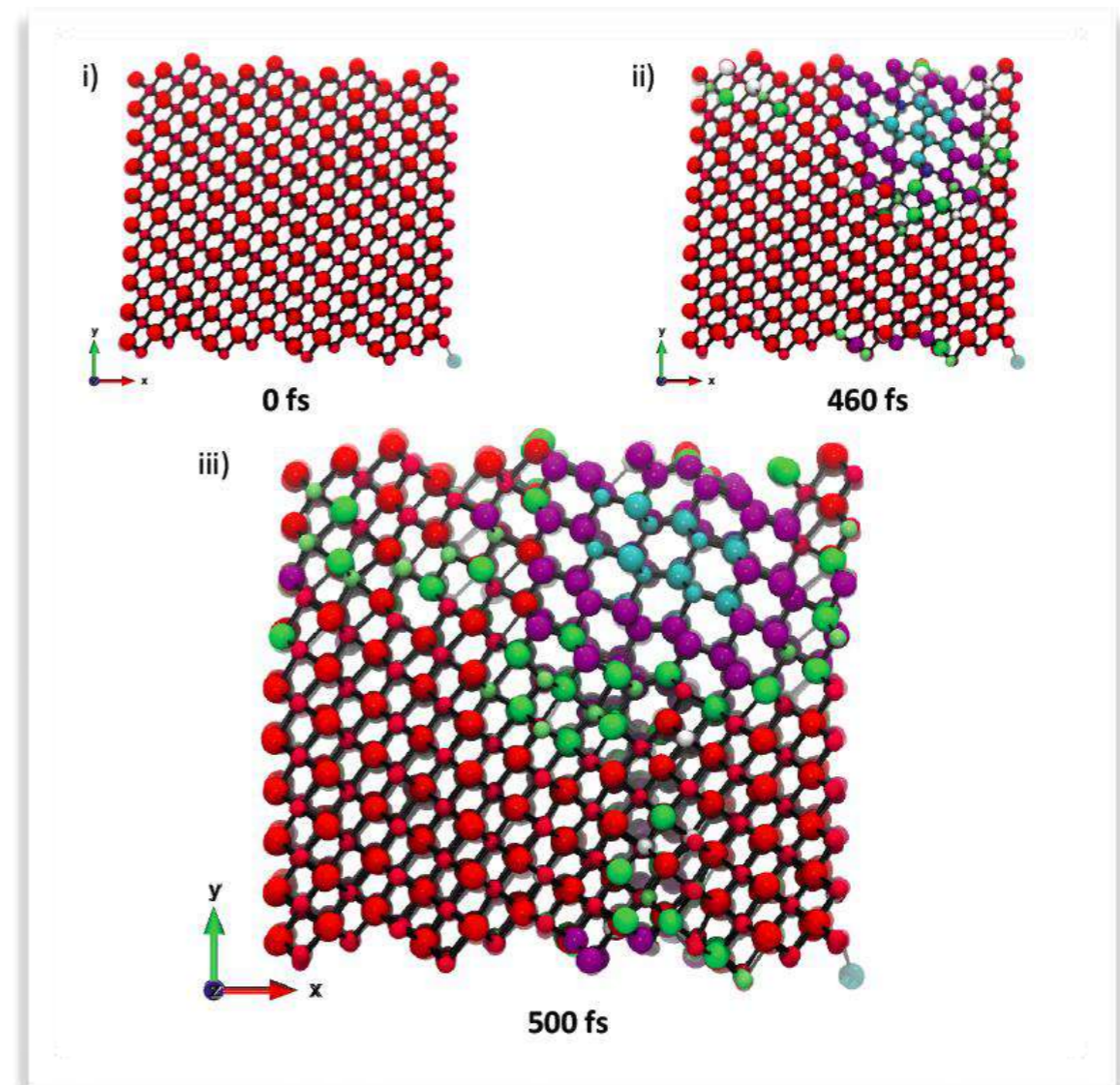
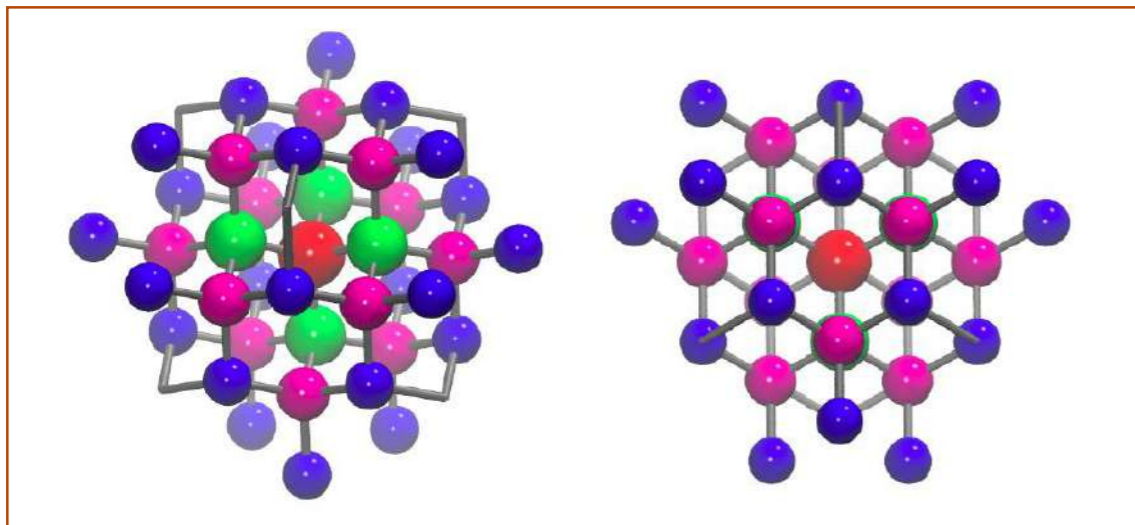
# Monte Carlo in Trajectory Space



„Shooting Algorithm“ (C. Dellago, D. Chandler)

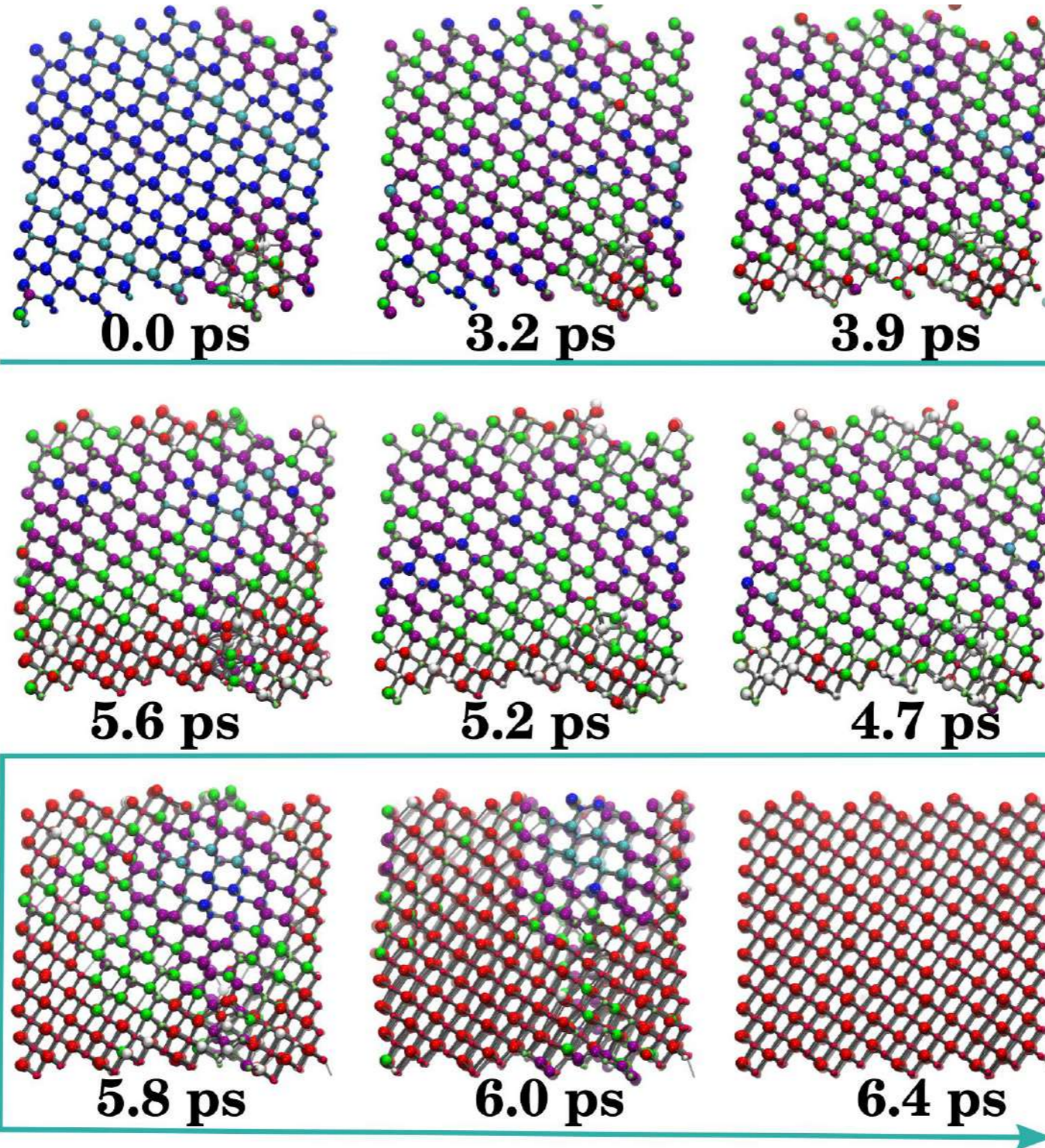


# Order Parameter (CV) - coordination number/sequence



# Mechanism from TPS - forwards

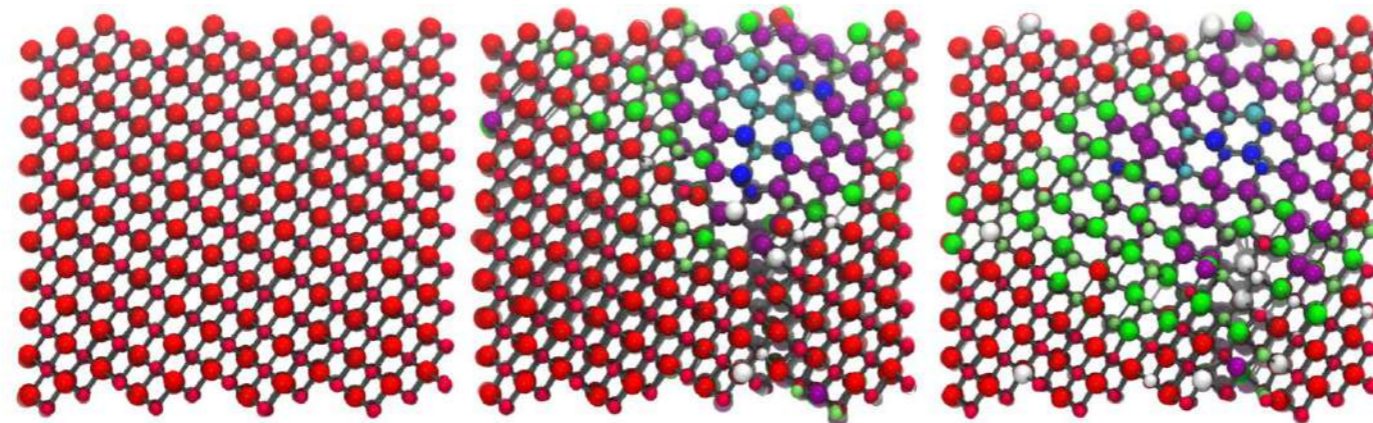
B3



B1

# Mechanism from TPS - backwards

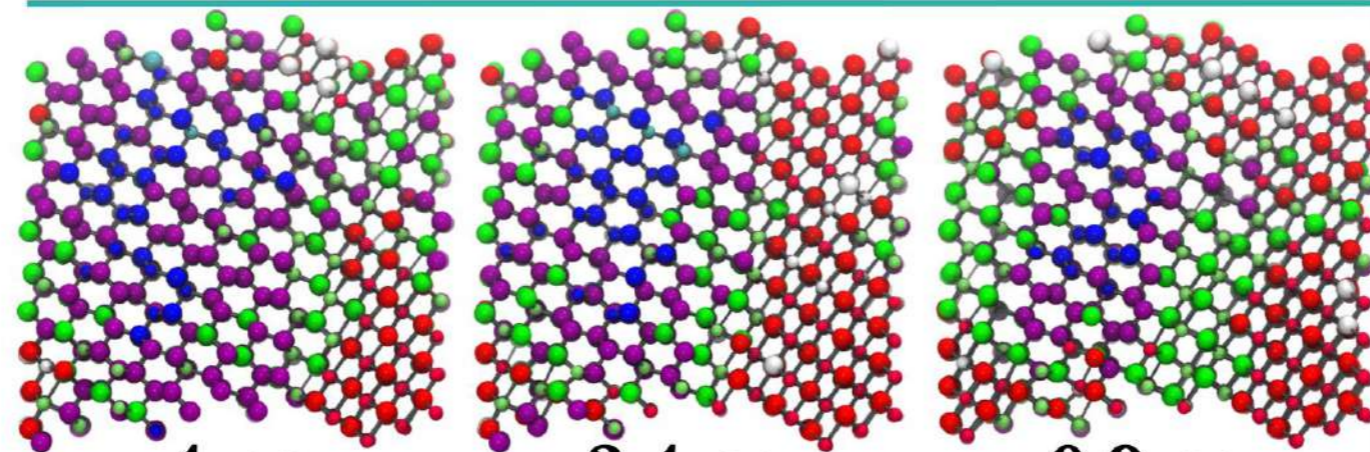
B1



0 ps

0.6 ps

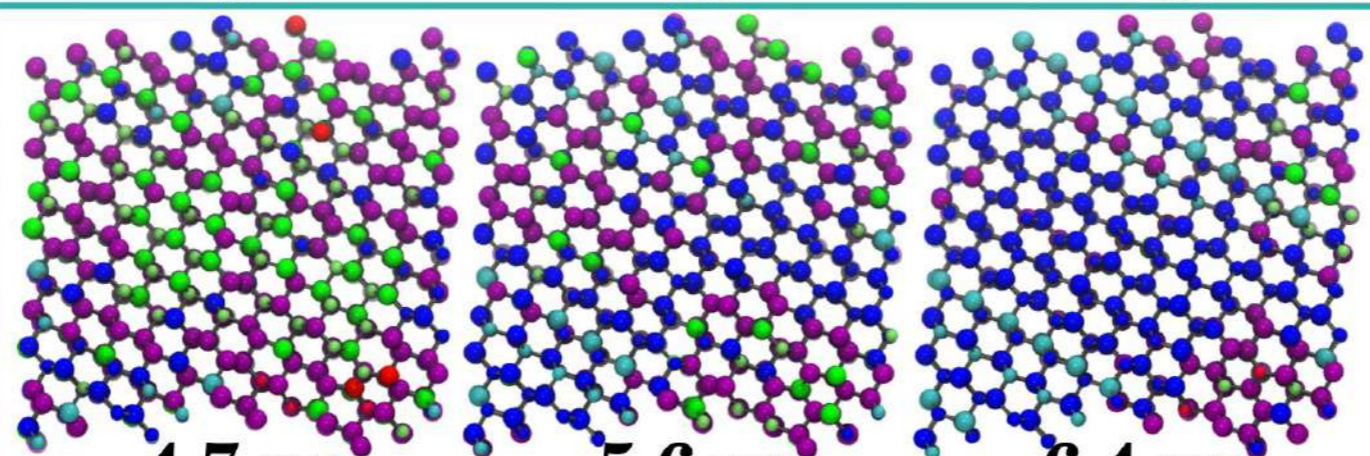
0.7 ps



4 ps

3.4 ps

0.9 ps



4.7 ps

5.6 ps

6.4 ps

B4/B3

# Free Energy Reconstruction (TPS/metaD)

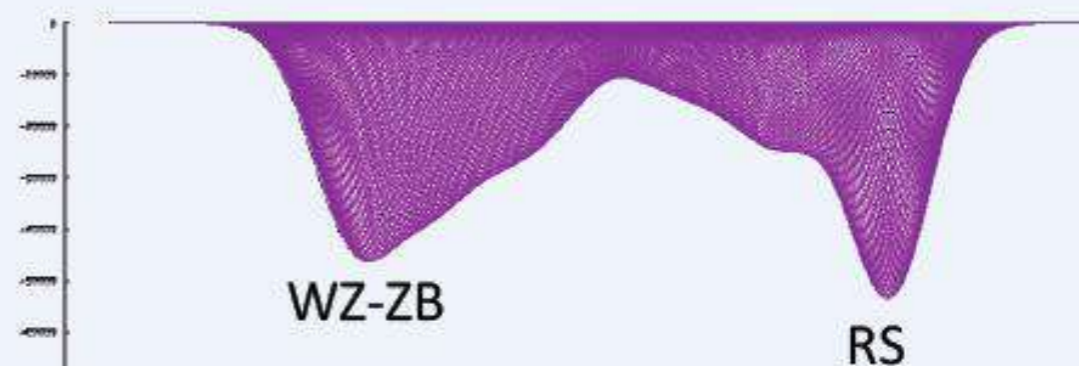
ZnO

a) Iteration 1

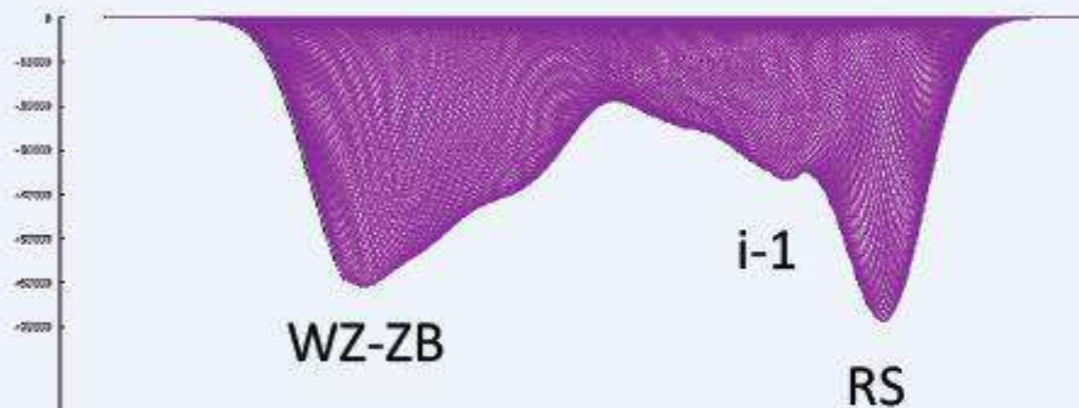


filling both basins

b) Iteration 50



c) Iteration 150



d) Iteration 200



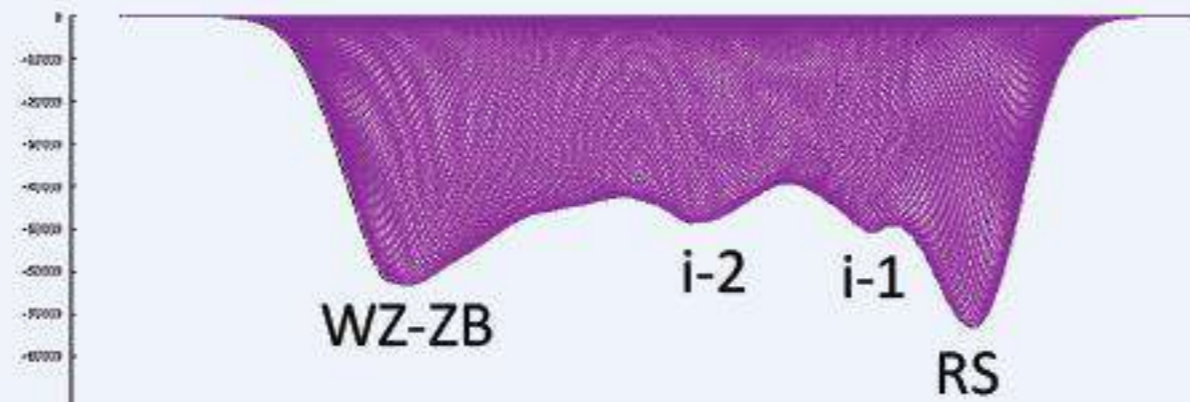
CV controlled by TPS,  
PE filling by Gaussians



1. **TPS step 1**: shoot off a new trajectory and time propagate.
2. **MetaD step 1**: deposit a bias using a metadynamics scheme, locally partially filling the as yet uncharacterised energy well.
3. **TPS step 2**: Generate another trajectory (as in step 1) and propagate into the now biased basin A, to generate a true MD velocity distribution on the biased potential.
4. **TPS step 3**: shoot off a new trajectory from the same snapshot as above and propagate, only this time backwards in time, to basin B.
5. **MetaD step 2**: In basin B, apply the same metadynamics scheme as above for a number of steps, in order to partially fill this second basin of attraction.
6. **TPS step 4**: Re-shoot a novel trajectory from a random snapshot of the previous trajectory. Propagate into the now biased basin B.

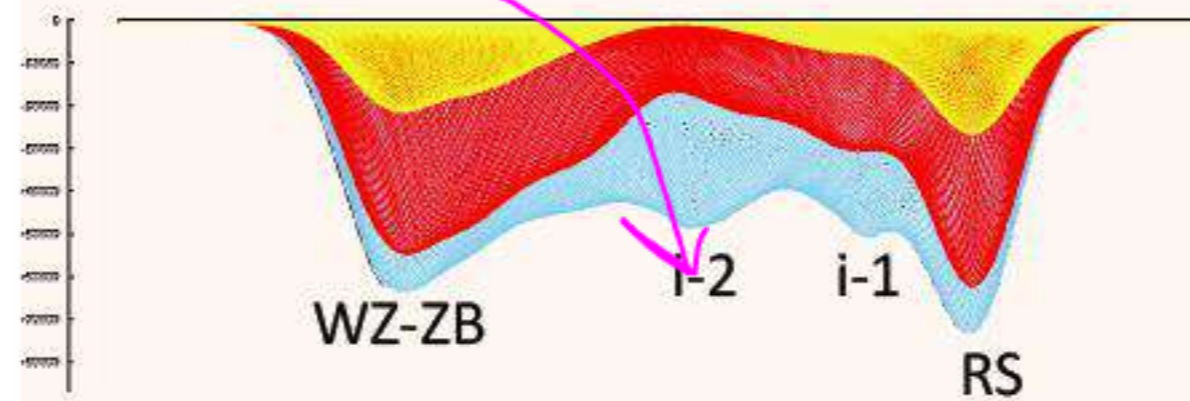
Repeat the above iterations of metadynamics and TPS moves, until the underlying free energy profile is fully converged.

**e) Iteration 225**



structuring of intermediate regions

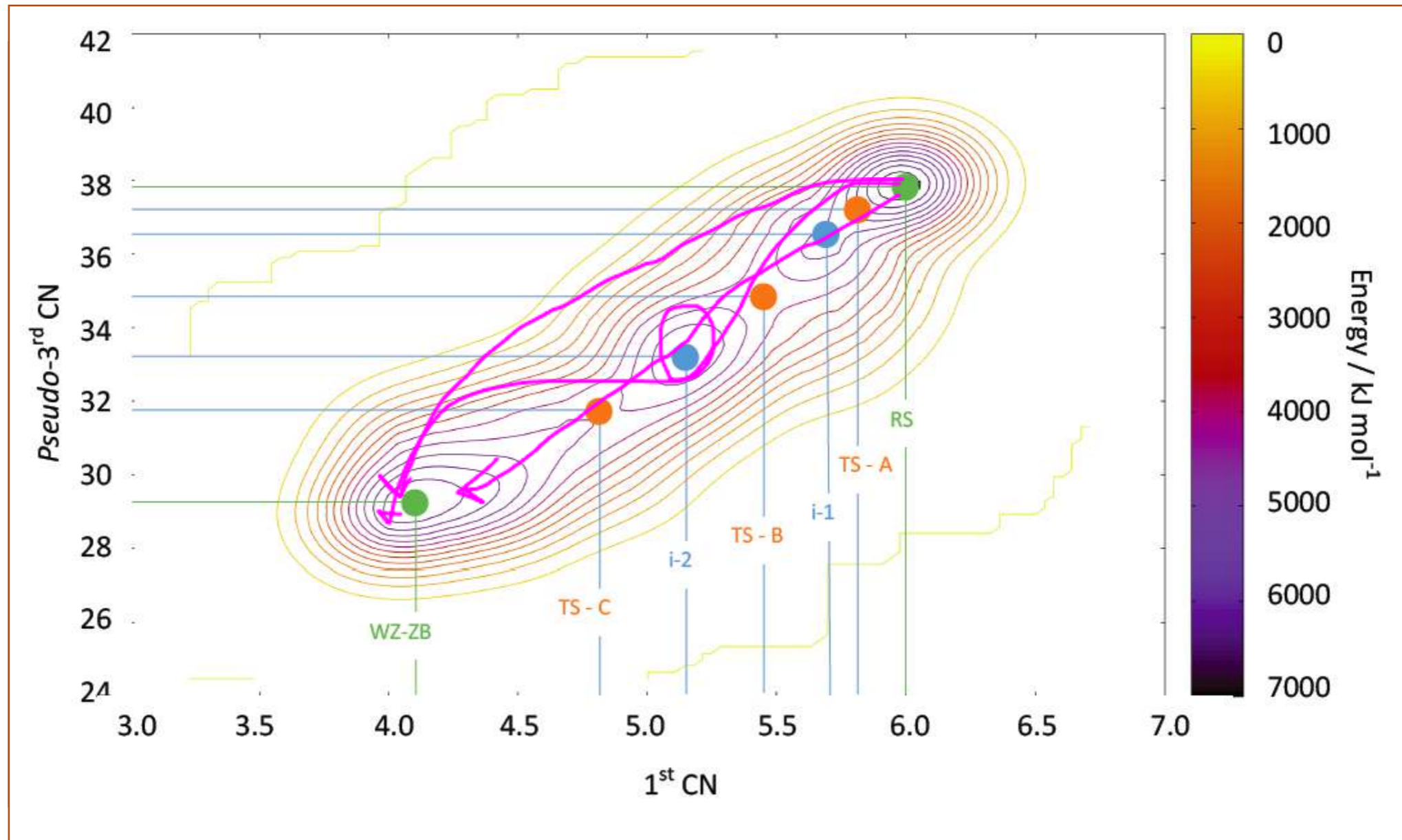
**f) Energy Comparison**

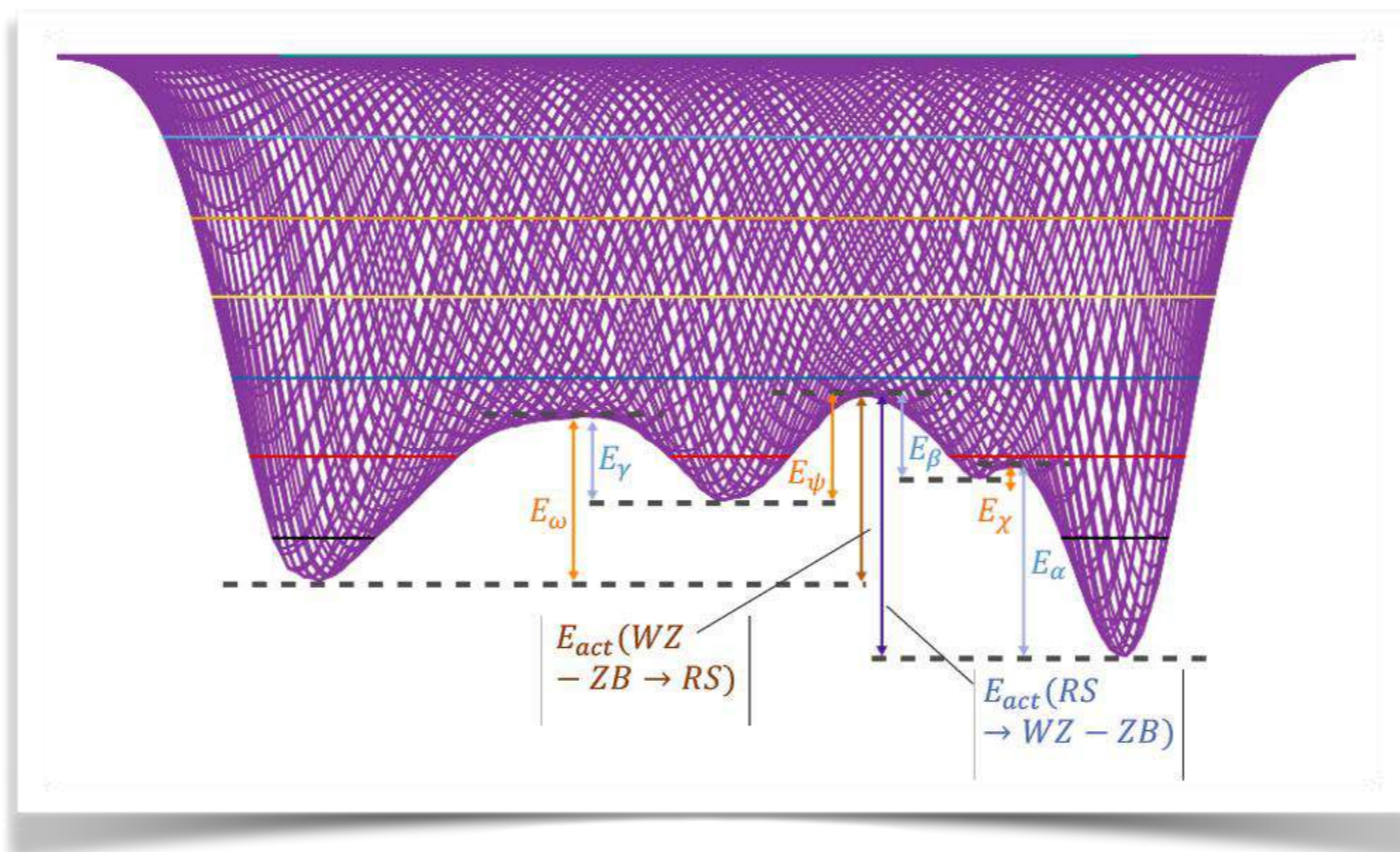


Iterations 10 (yellow), 75 (red), 225 (blue)

Population of intermediate basins in the late stage only

# 2D map of two-dimensional CV





|  | Energy /kJ mol <sup>-1</sup> | Energy /kJ mol <sup>-1</sup> pair <sub>1</sub> <sup>-1</sup> | Energy /eV pair <sup>-1</sup> | Energy /k <sub>B</sub> T pair <sup>-1</sup> |
|--|------------------------------|--|-------------------------------|---|
|--|------------------------------|--|-------------------------------|---|

|            |          |      |      |     |
|------------|----------|------|------|-----|
| $E_\chi$   | 20 447.0 | 17.1 | 0.18 | 6.8 |
| $E_\psi$   | 13 085.9 | 10.9 | 0.11 | 4.4 |
| $E_\omega$ | 1 357.0  | 1.3  | 0.01 | 0.5 |

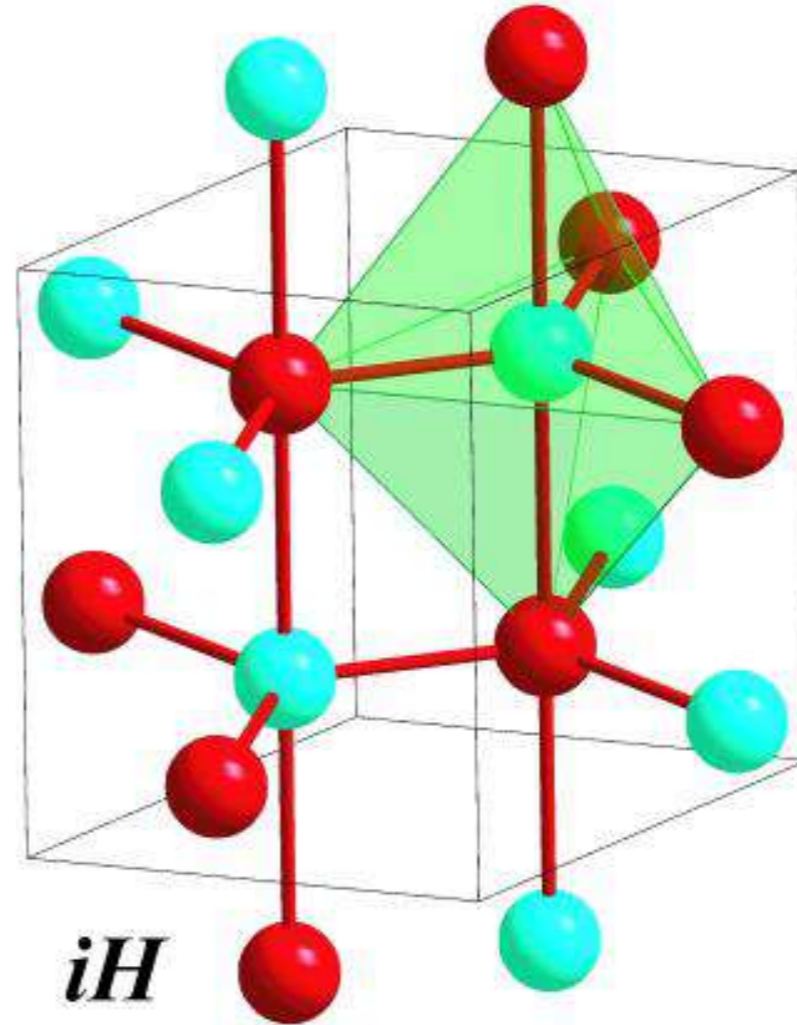
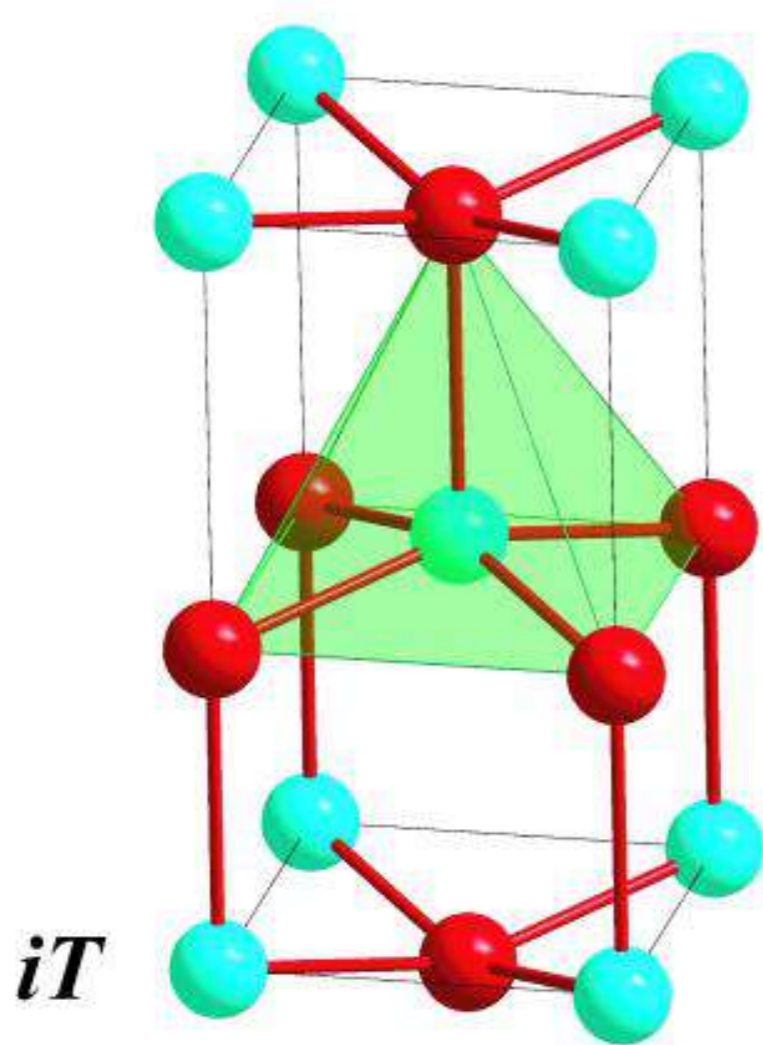
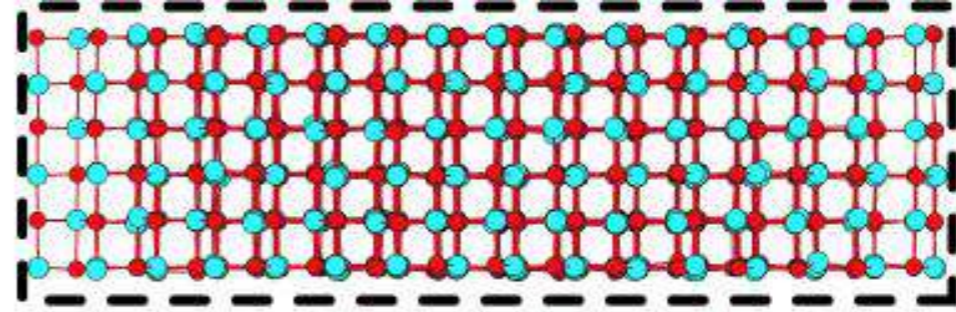
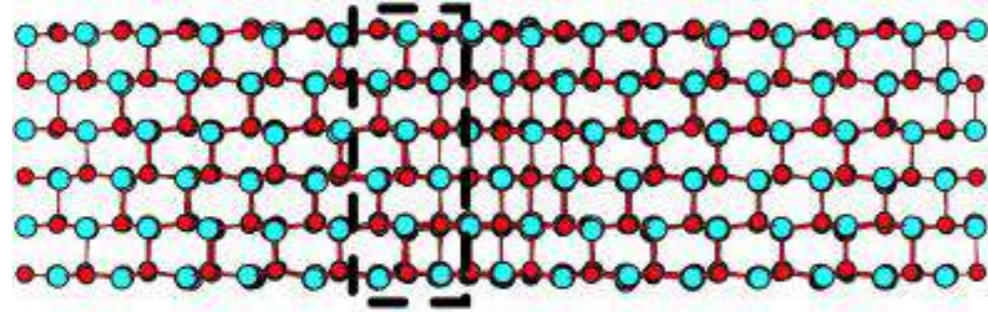
|                                   |          |      |      |     |
|-----------------------------------|----------|------|------|-----|
| $E_{act}(WZ - ZB \rightarrow RS)$ | 23 049.1 | 19.2 | 0.20 | 7.7 |
|-----------------------------------|----------|------|------|-----|

|  | Energy /kJ mol <sup>-1</sup> | Energy /kJ mol <sup>-1</sup> pair <sub>1</sub> <sup>-1</sup> | Energy /eV pair <sup>-1</sup> | Energy /k <sub>B</sub> T pair <sup>-1</sup> |
|--|------------------------------|--|-------------------------------|---|
|--|------------------------------|--|-------------------------------|---|

|            |          |      |      |     |
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|                                   |          |      |      |      |
|-----------------------------------|----------|------|------|------|
| $E_{act}(RS \rightarrow WZ - ZB)$ | 32 565.9 | 27.1 | 0.28 | 10.9 |
|-----------------------------------|----------|------|------|------|

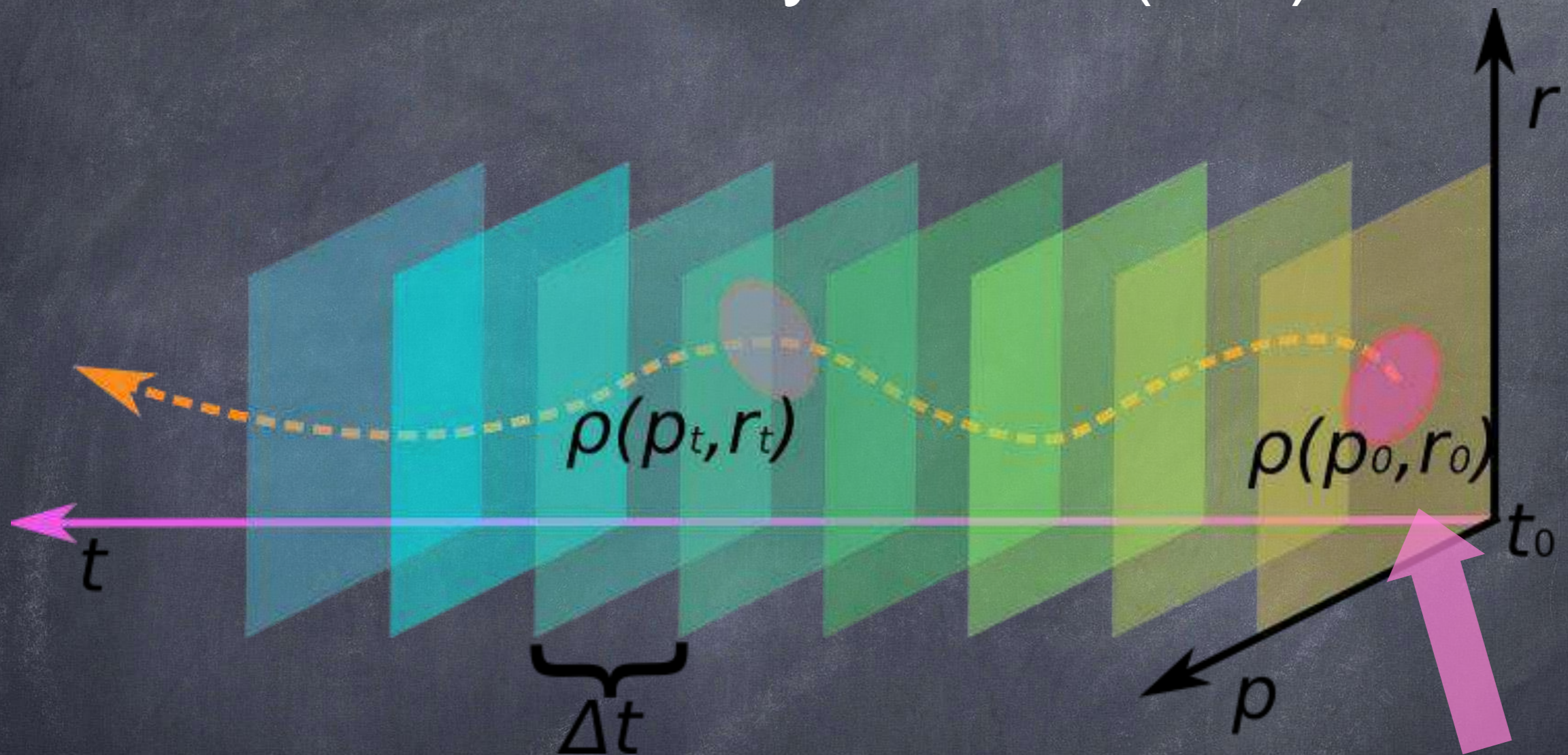
# i2 - intermediate



# Workshop 2

- Examples from metaD and TPS
- Details of the *shooting* approach
- Details of MD engines

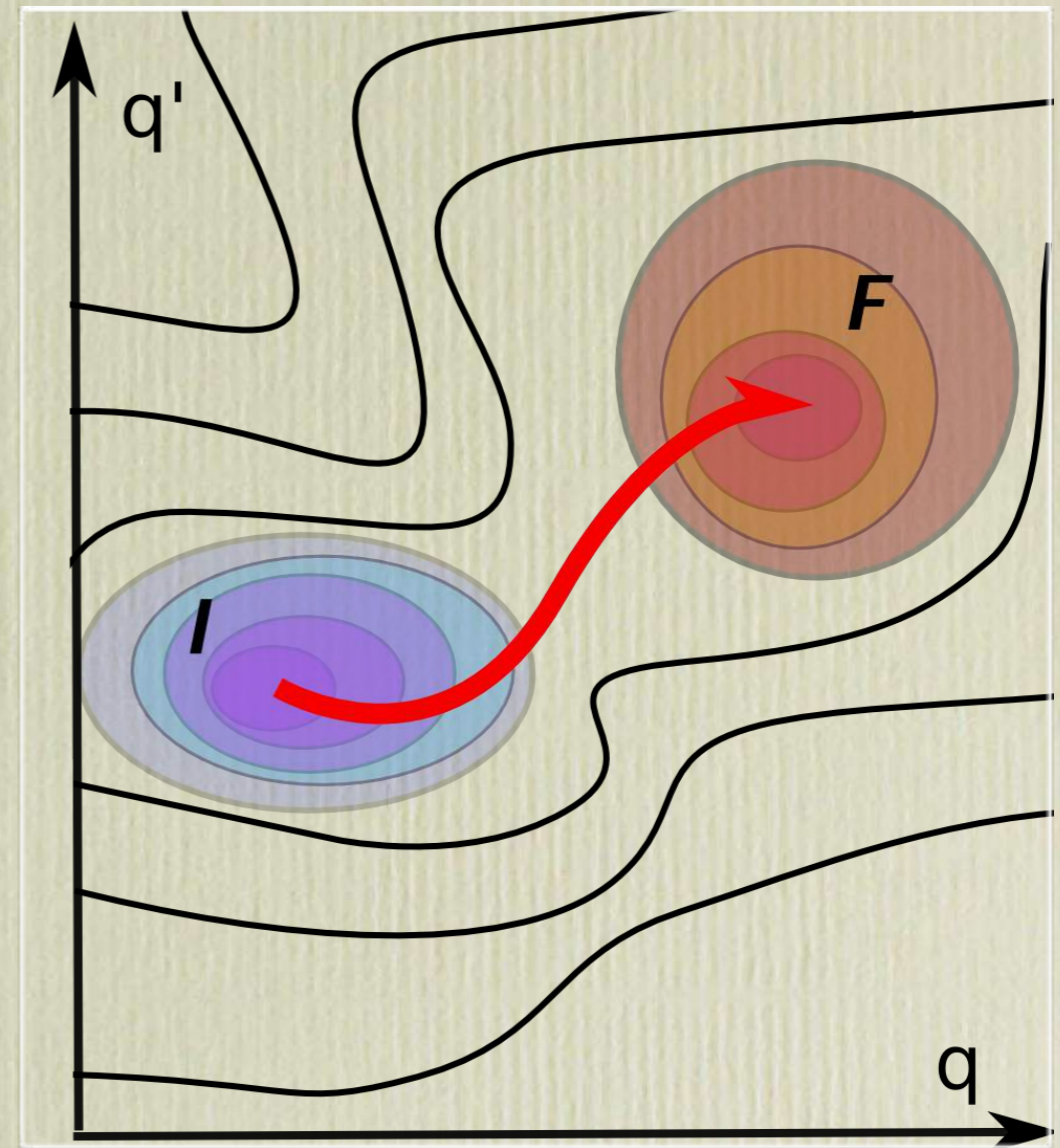
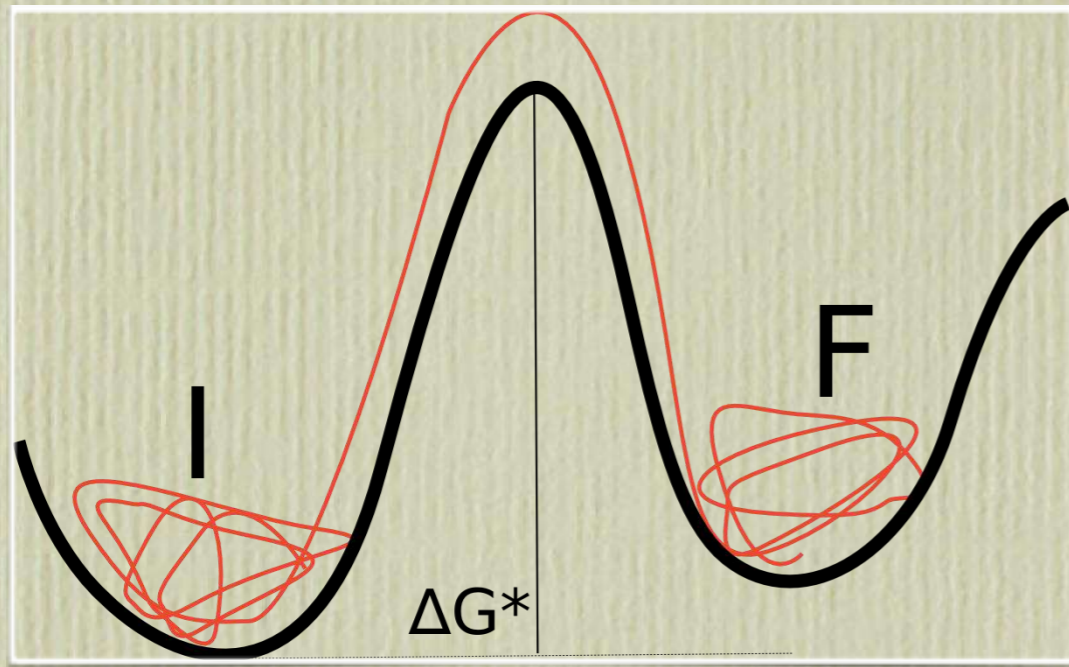
# Time-Evolution of a System Molecular Dynamics (MD)



Calculate forces on atoms and propagate in time

Initial configuration:  
Specify positions and velocity distribution at temperature  $T$ .

# Different time scales (MD)



*Frequent and slow vs.  
Rare and quick*

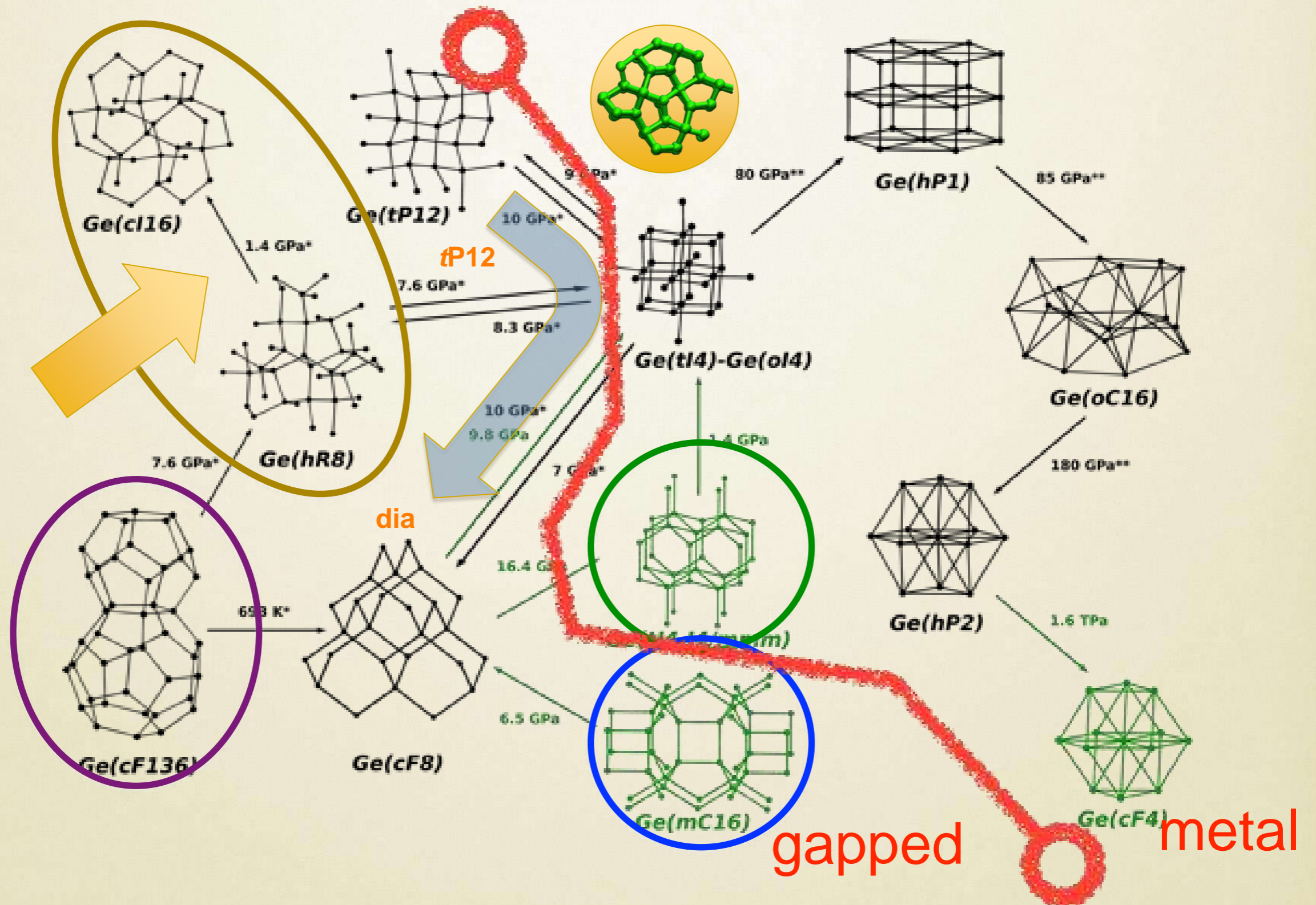


MetaD 1

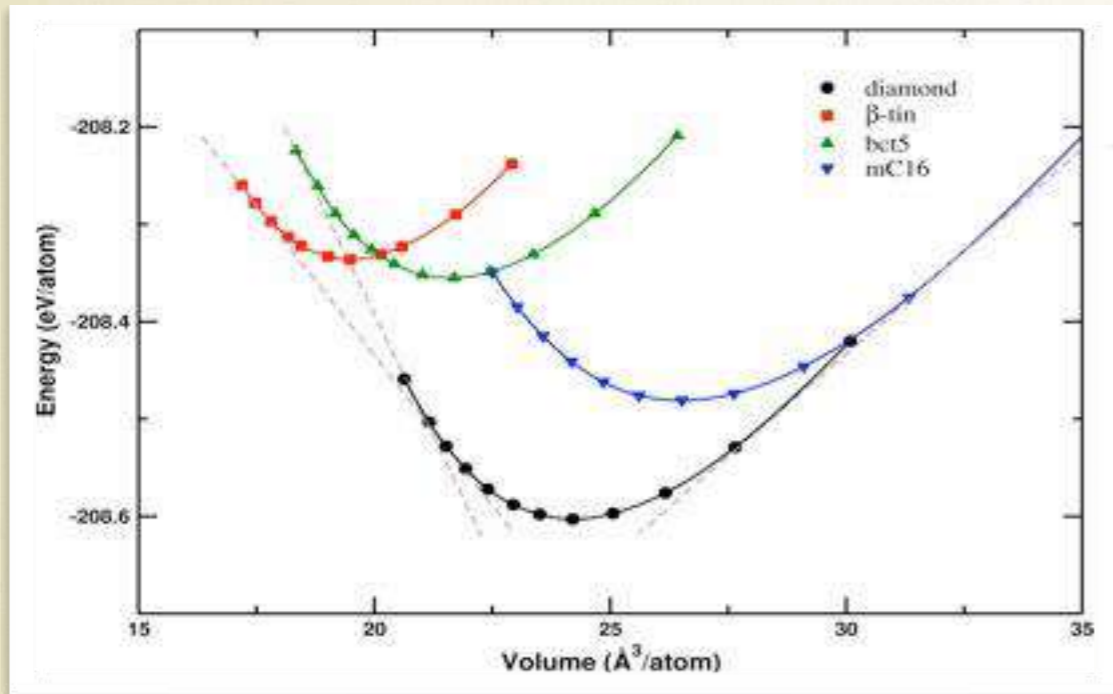
# Details

- siesta as MD/Force engine (DFT)
- box as CV
- external driver (metaD)
- chain of NVT - metaD - NVT simulations

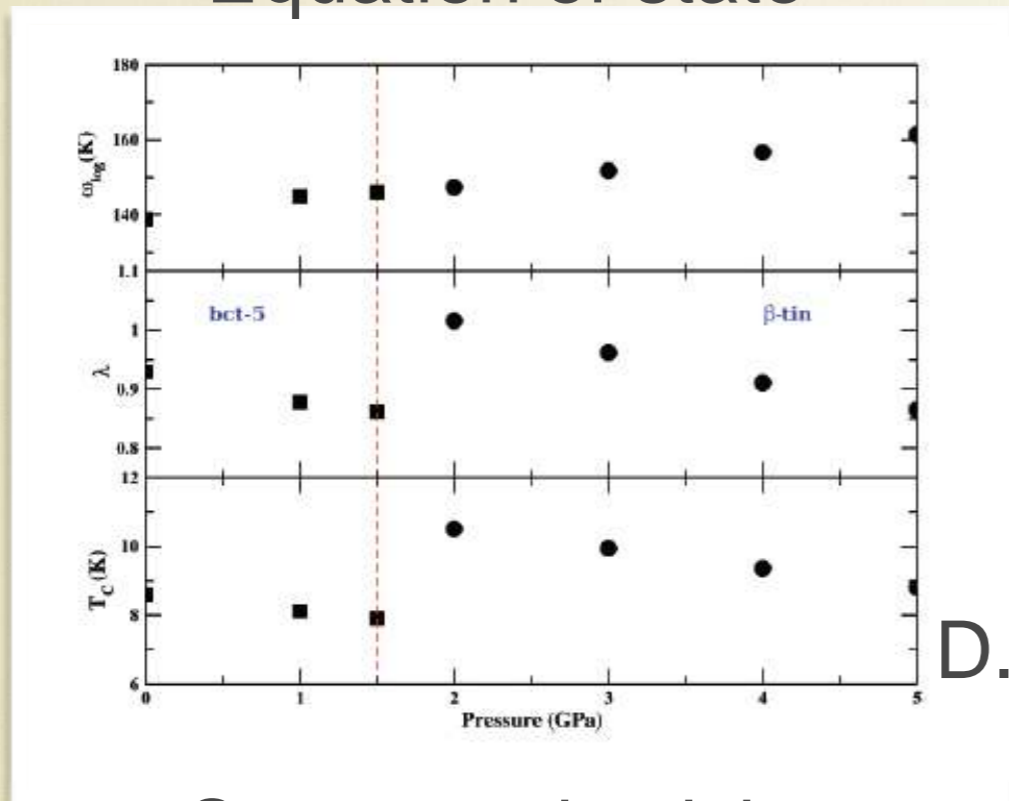
# Ge - Refinement of the Phase Diagram



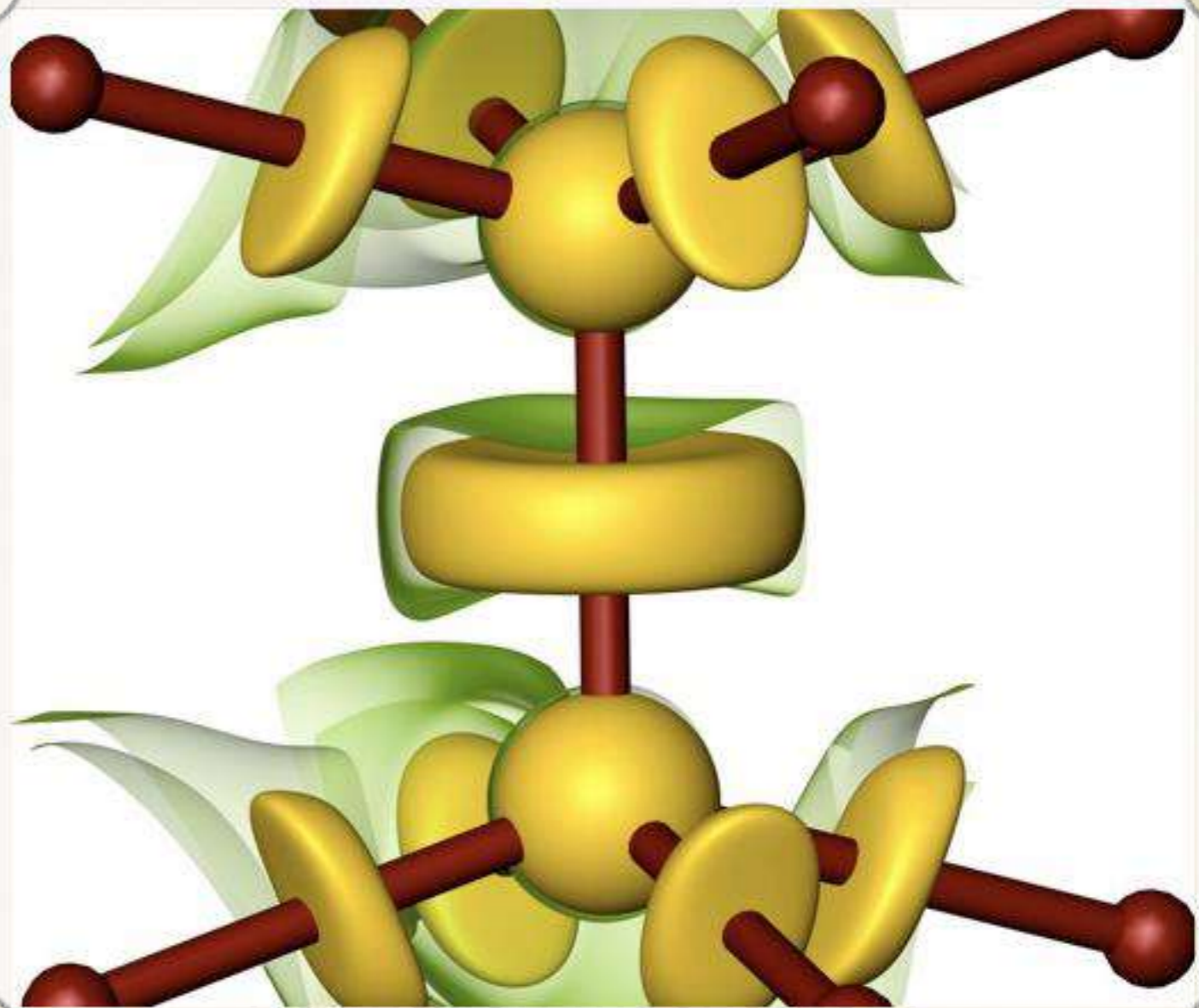
# Ge - Metallic & Superconducting



Equation of state



Superconductivity



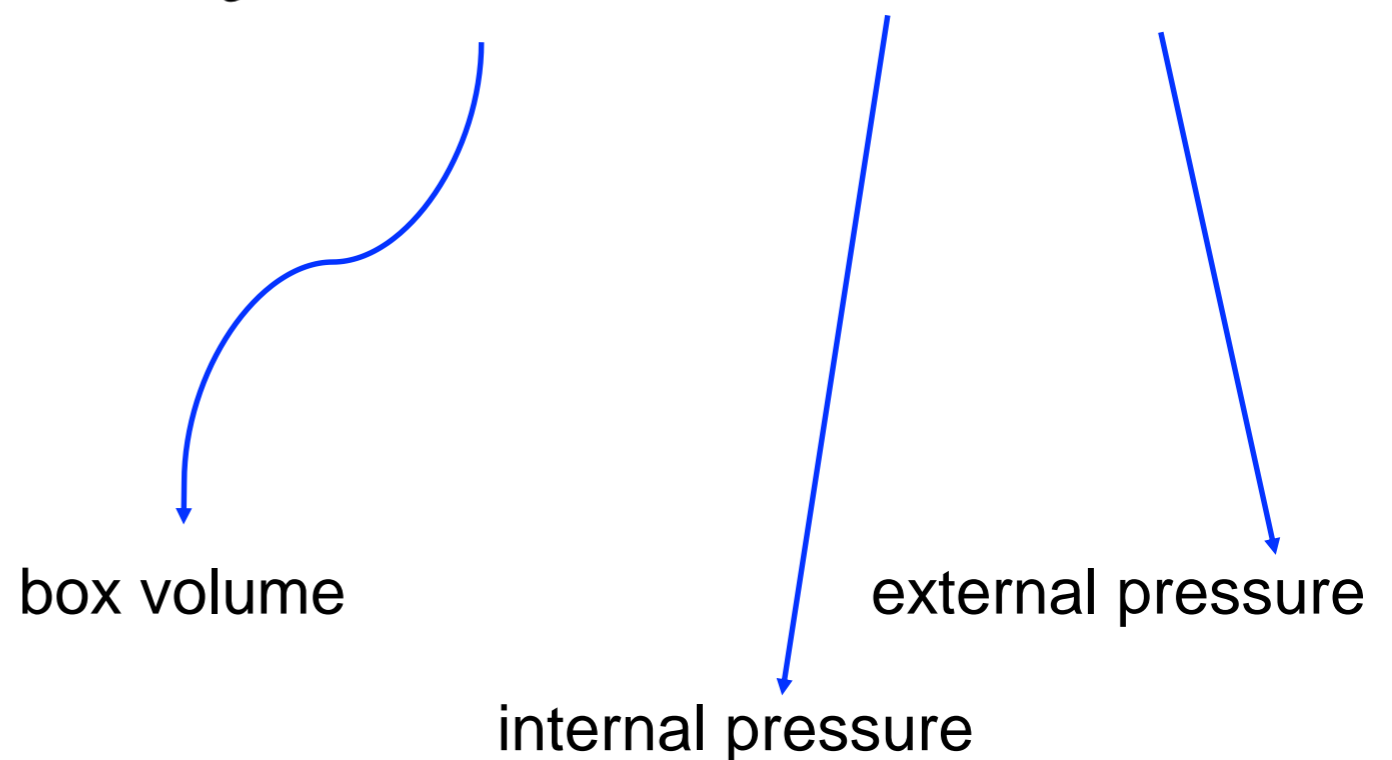
D. Selli *et al.*, Scientific Reports 3, 1466 (2013)

D. Selli *et al.*, [arXiv:1209.3753](https://arxiv.org/abs/1209.3753) (2012)

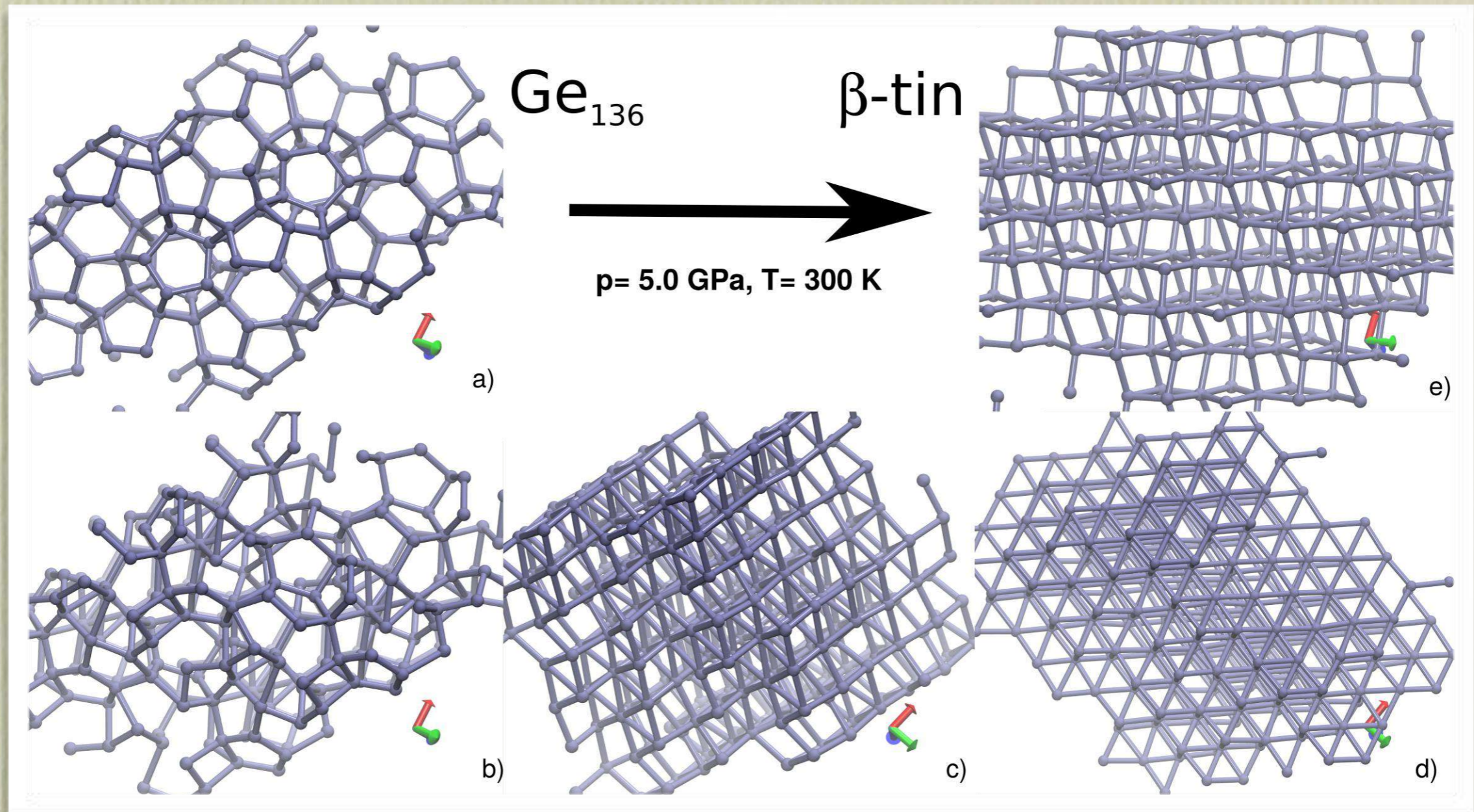
# Gibbs free energy

- Crystal structures correspond to minima of the **Gibbs free energy**  
 $G(\mathbf{h}) = F(\mathbf{h}) + PV$
- Different crystal structures, and different symmetries.
- MD simulation box matrix  $\mathbf{h}$  as order parameter
- **6 independent components** of the matrix  $\mathbf{h}$

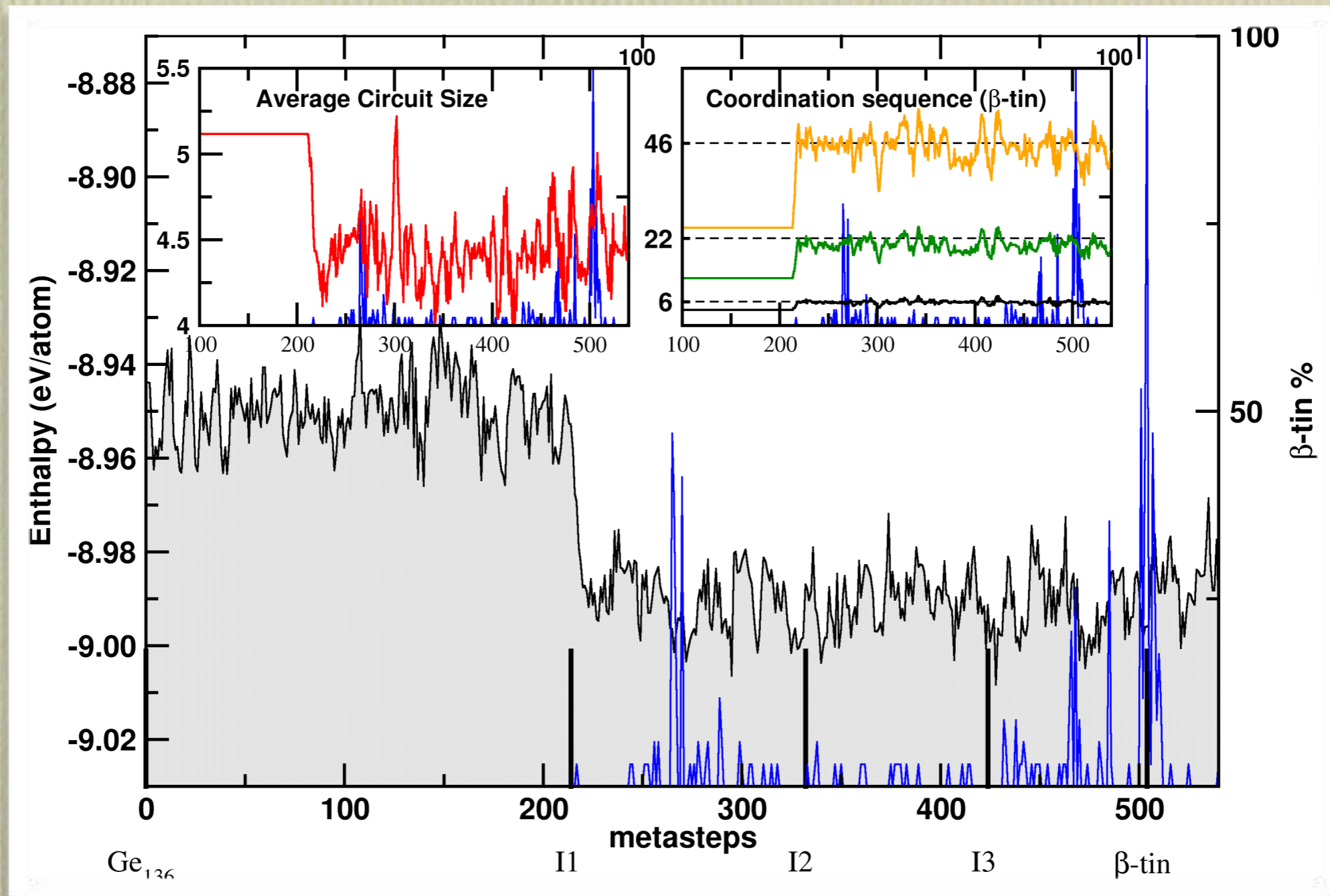
$$-\frac{\partial \mathcal{G}}{\partial h_{ij}} = V [\mathbf{h}^{-1} (\mathbf{p} - P)]_{ji}$$



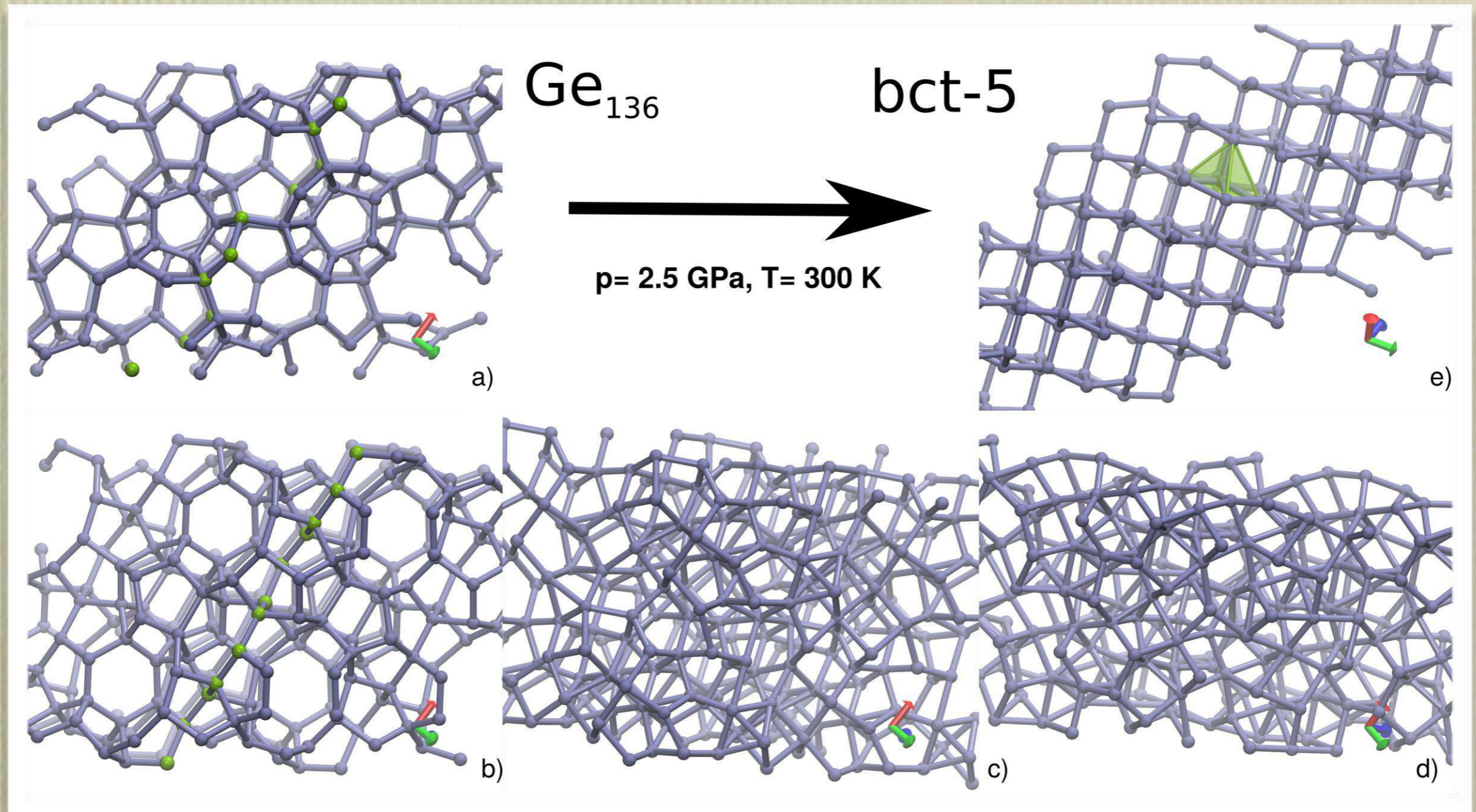
# Ge<sub>136</sub> (cF136) as precursor



# Ge<sub>136</sub> (cF136) as precursor

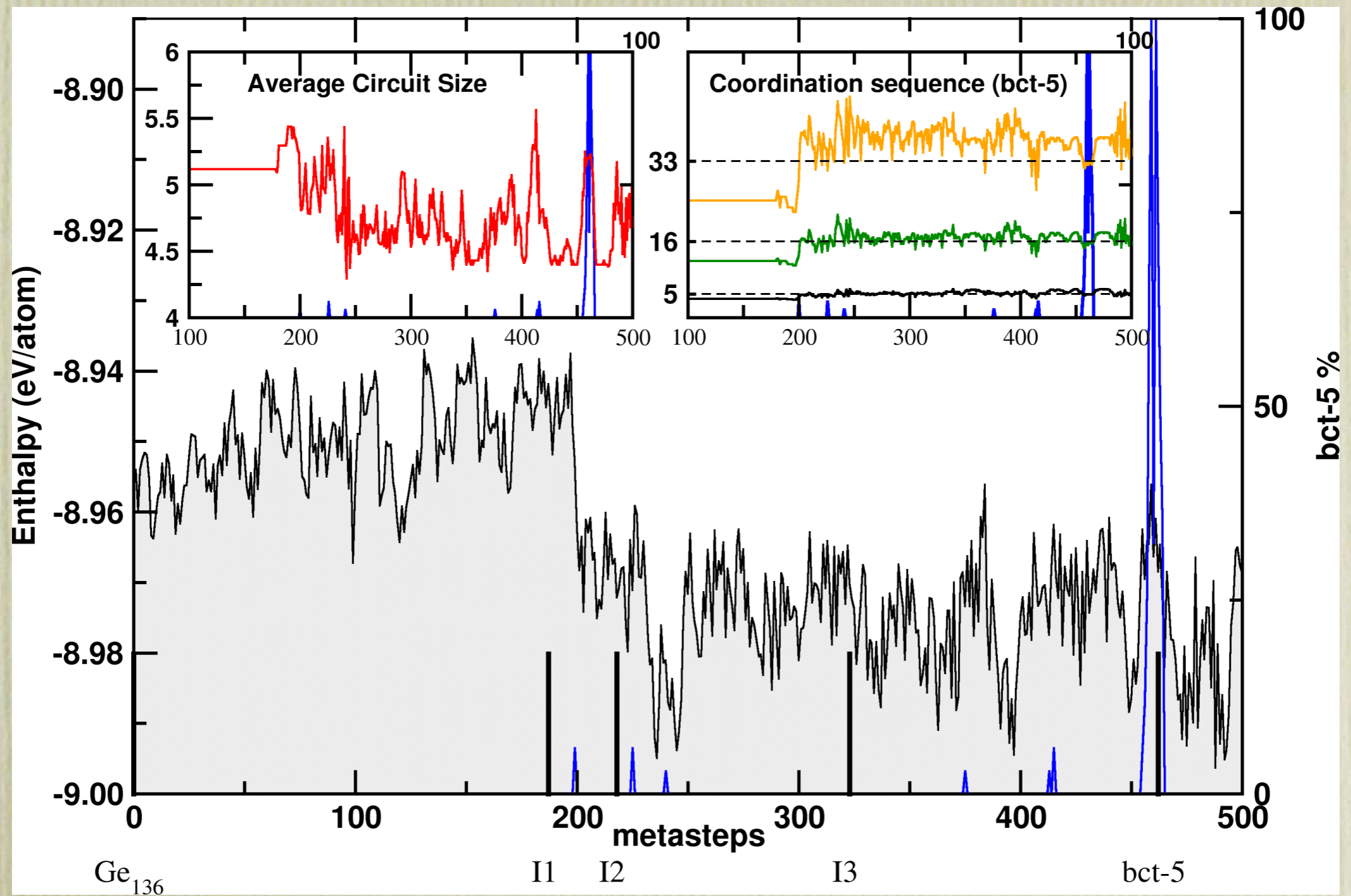


# Formation of bct-5

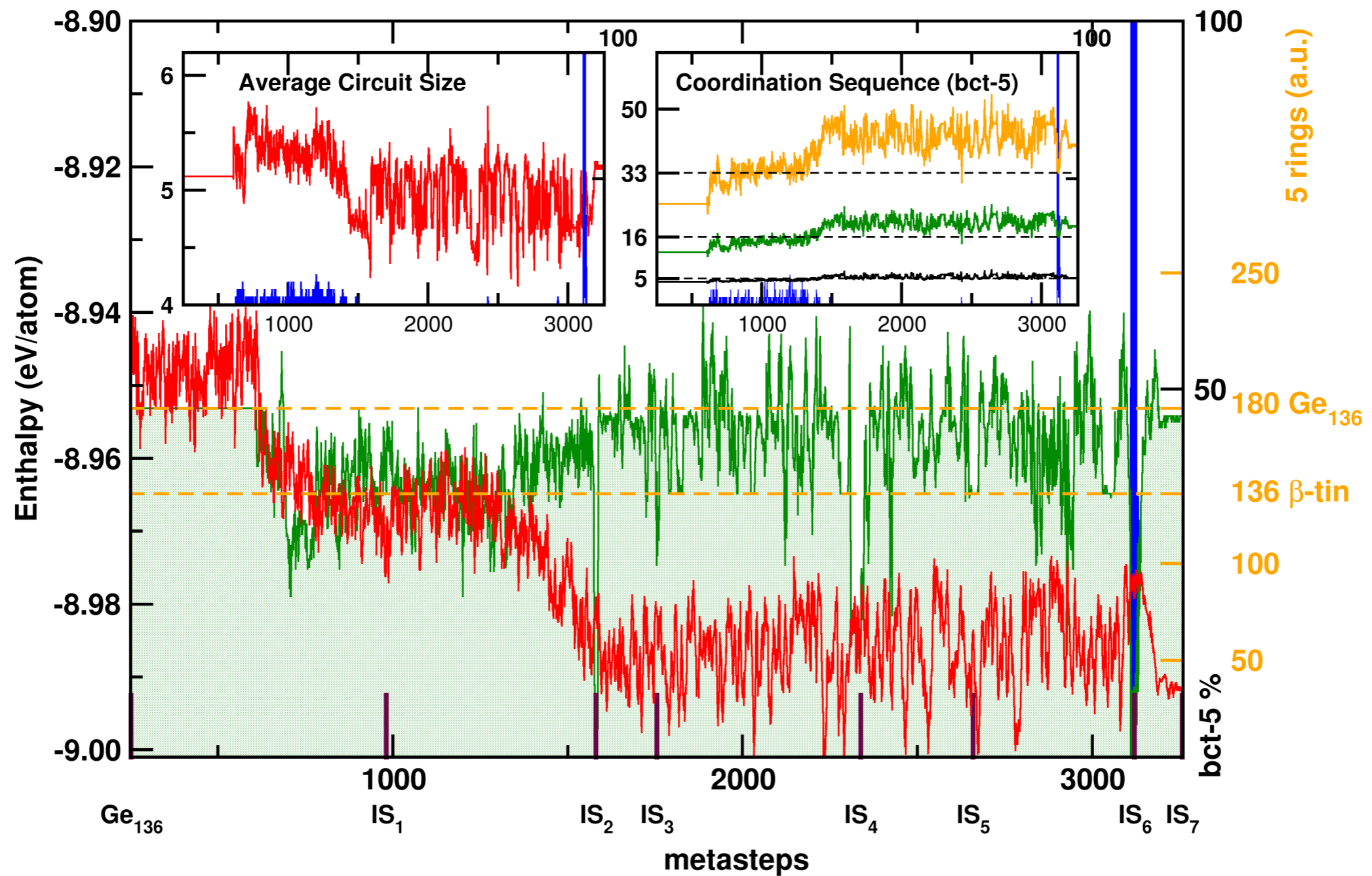




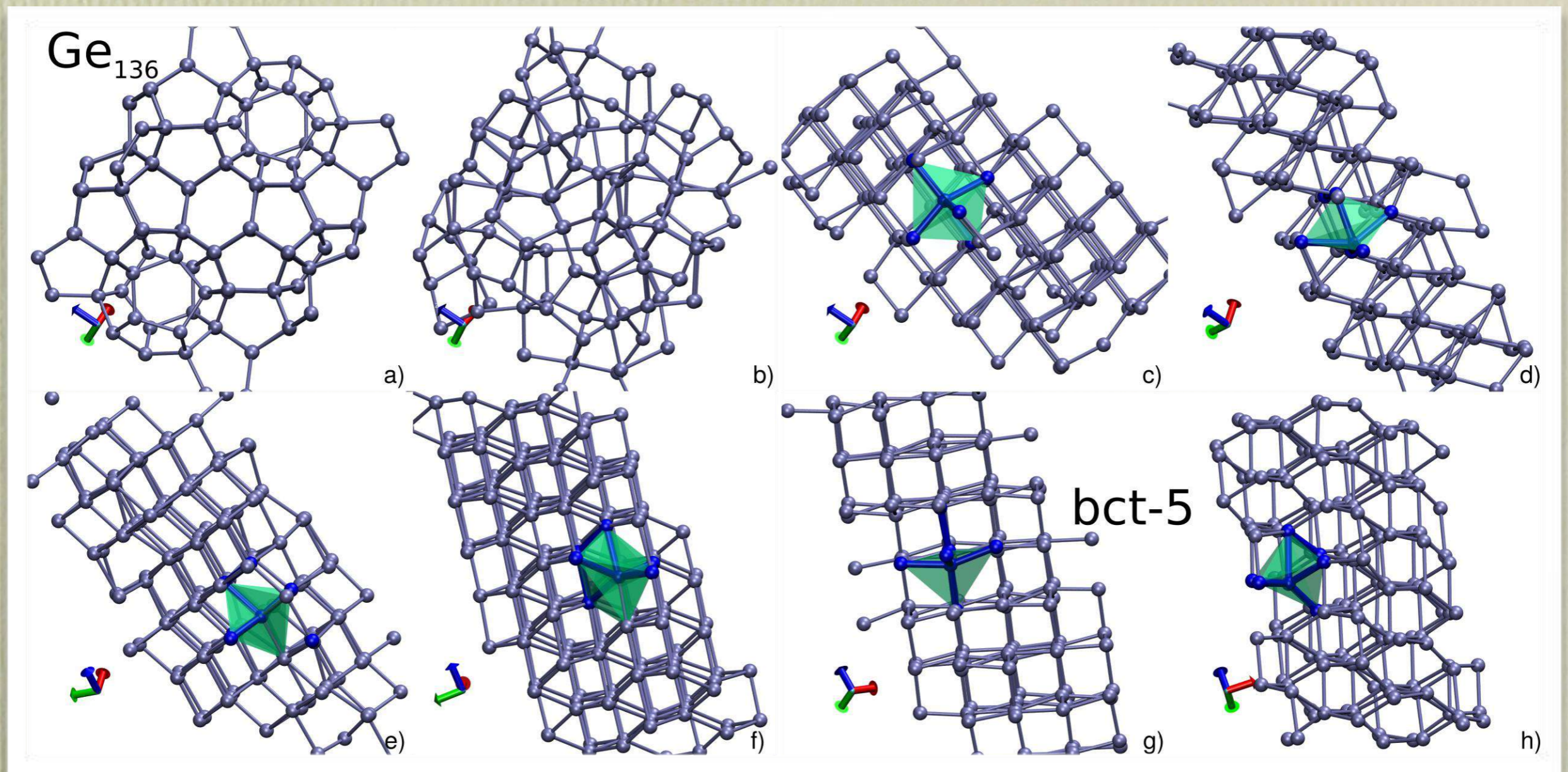
# Descriptors



# Low Temperature (77K)



# Metadynamics at 77K

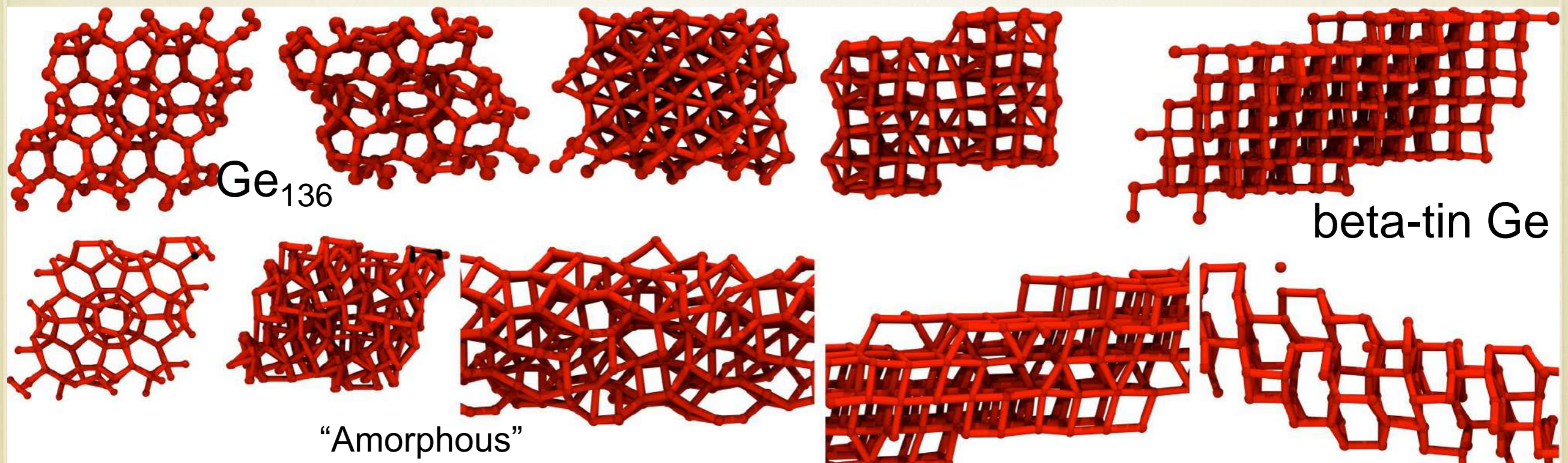


# Looking for a formation mechanisms

## Clathrate $\text{Ge}_{136}$

—> Control nucleation!

Higher Pressure, Room Temperature Path



Lower pressure, Low Temperature Path

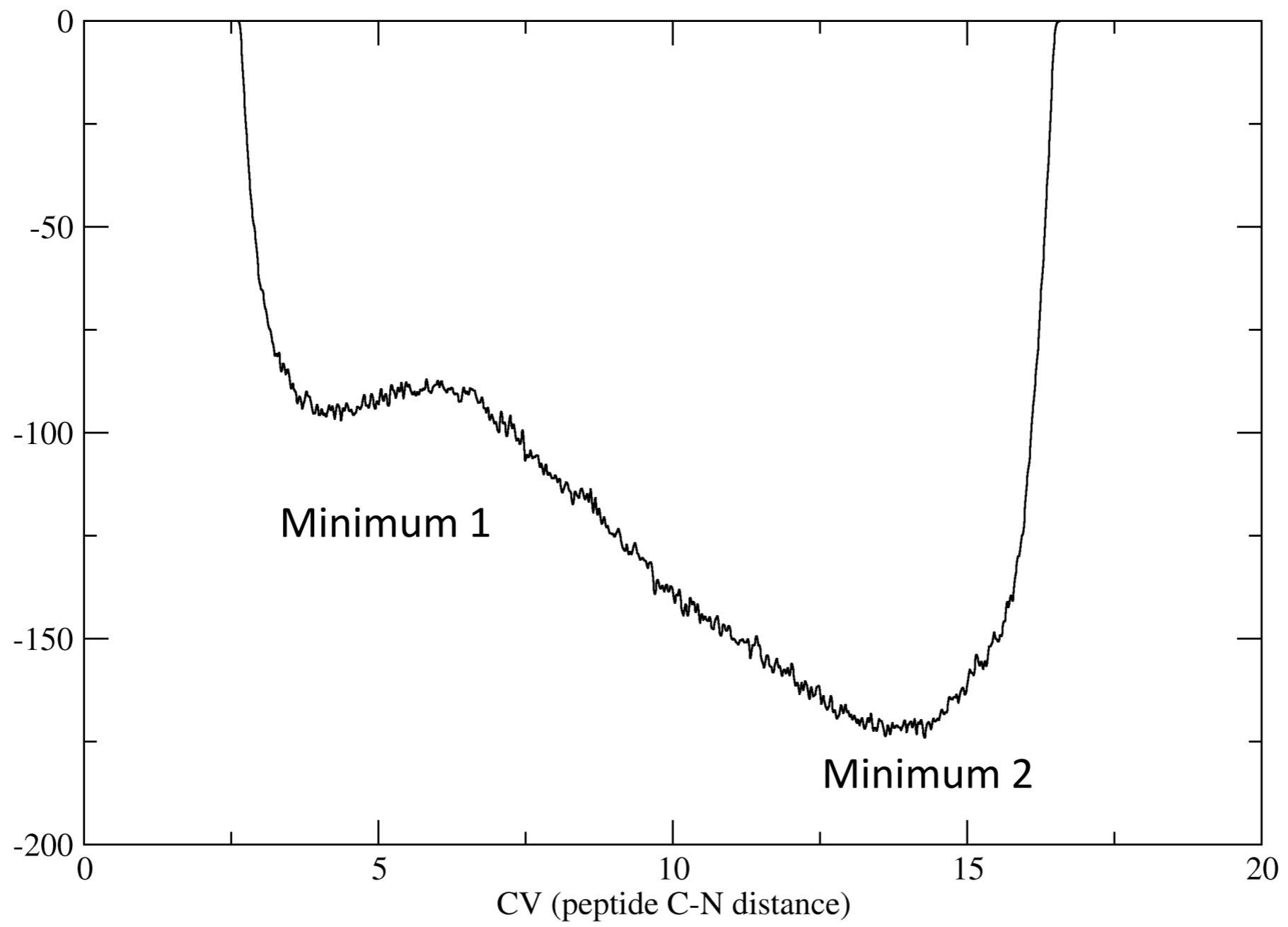
Different Paths, Intermediates & Nucleation History

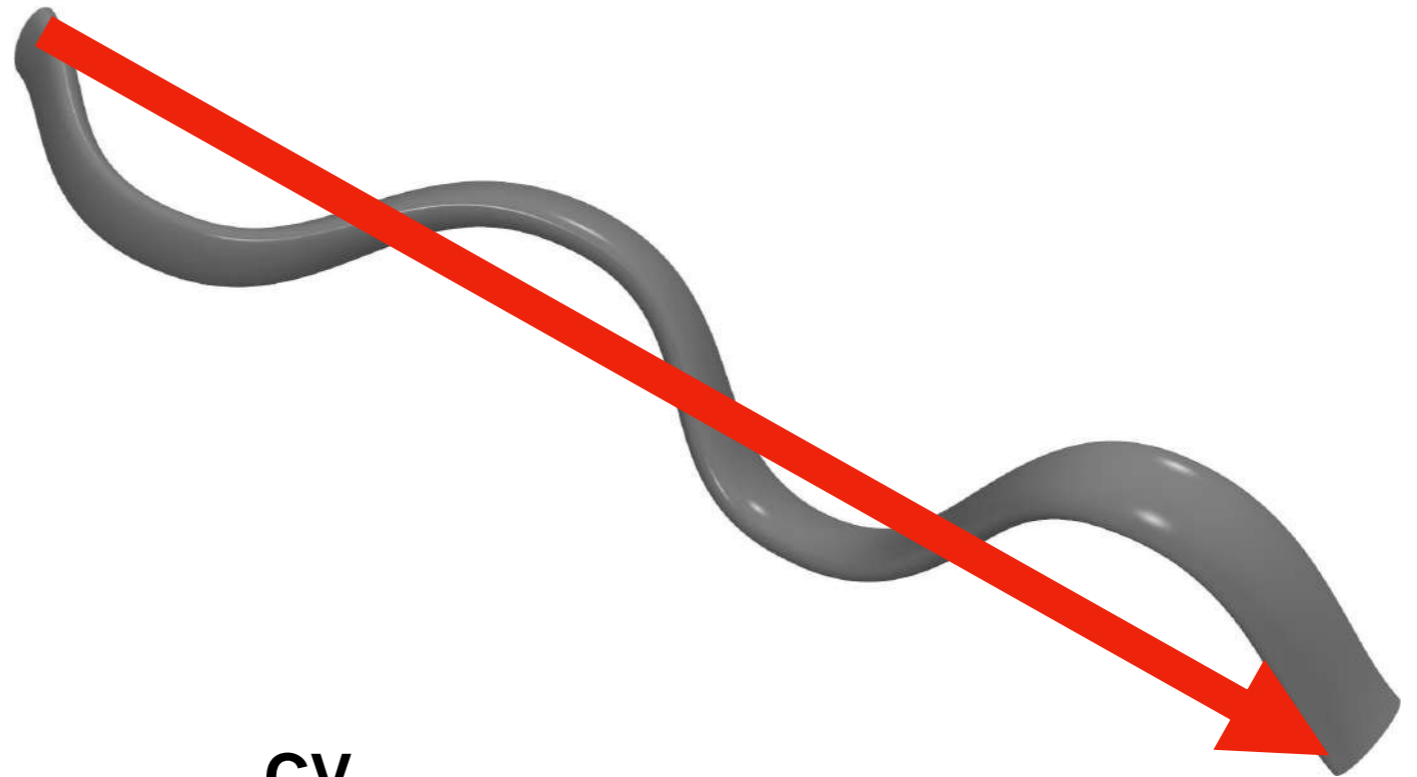
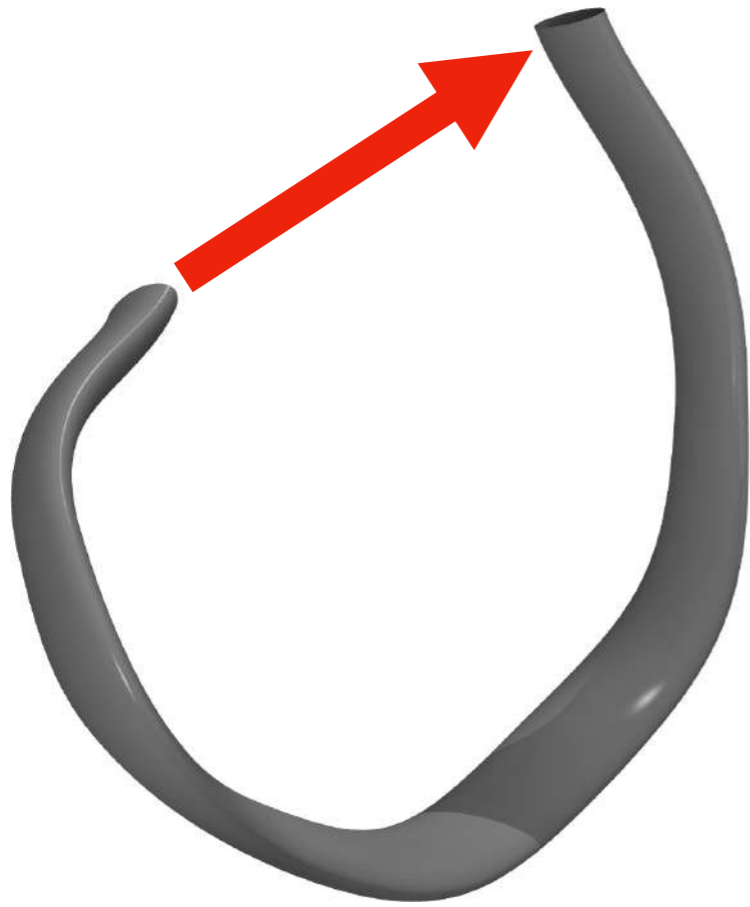
D. Selli *et al.* (2017), in preparation

MetaD 2

# Details

- cp2k as MD/Force
- based on FF (attempted with DFTB as QM/MM)
- external driver (plumed), distance as CV





**CV**



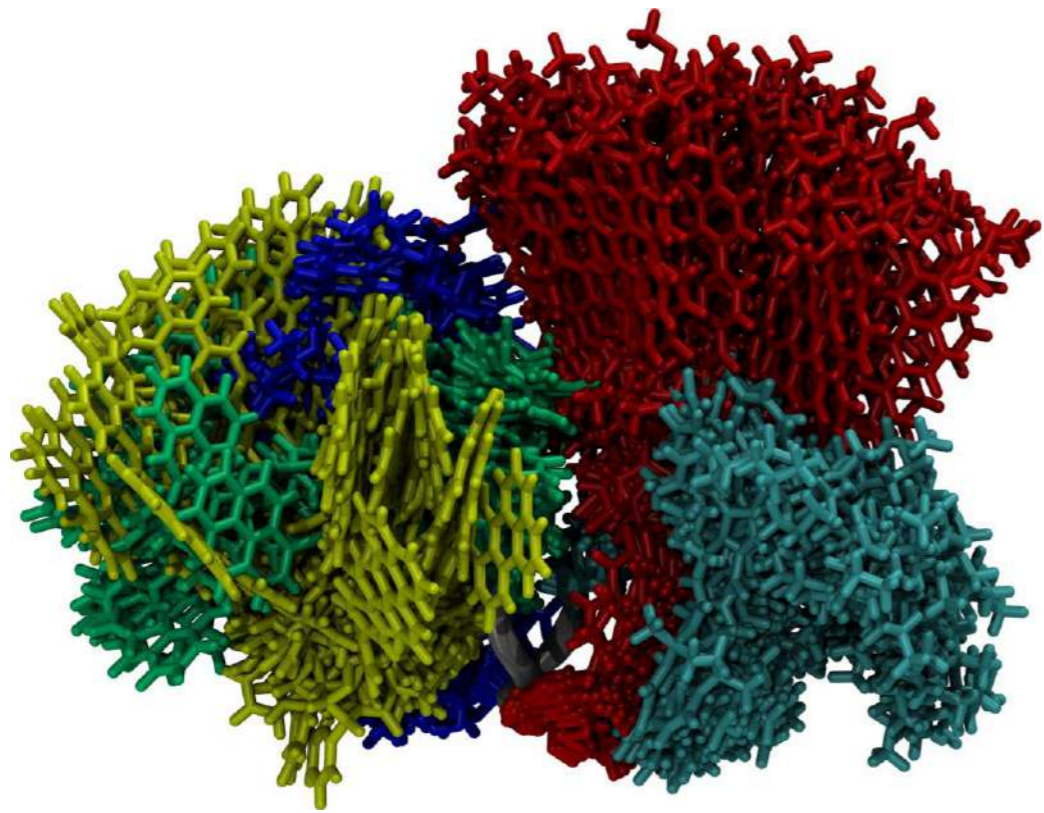
Min1 { within 1.0%  
within 0.5%

Free Energy -182.17 kJ/mol

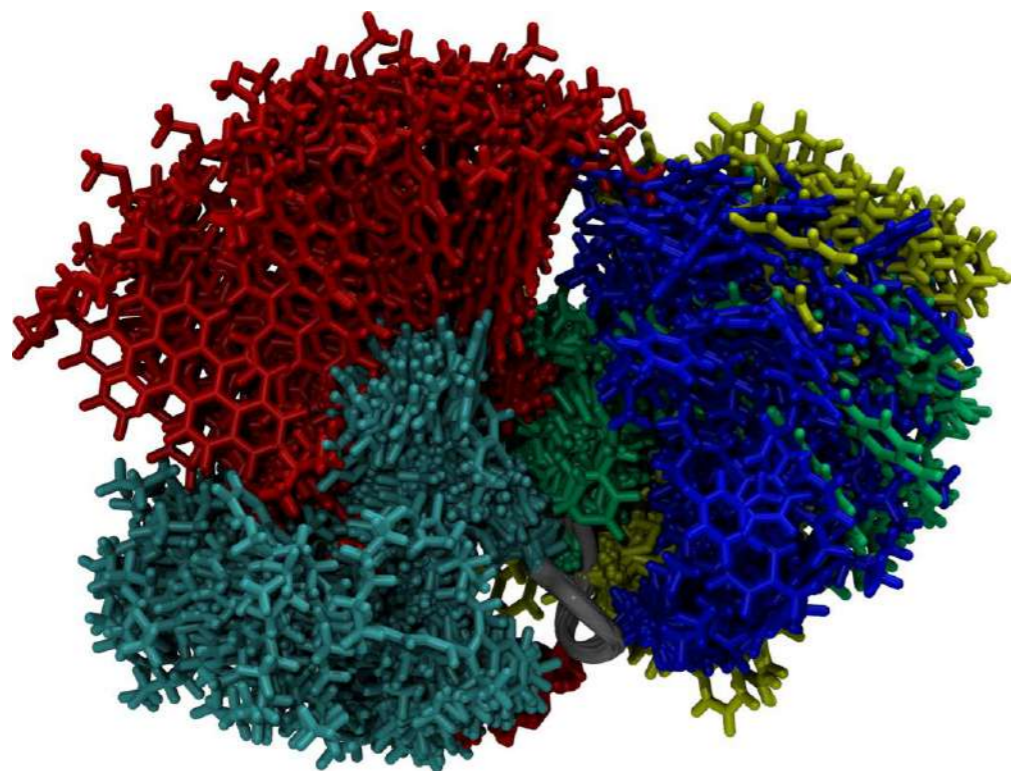
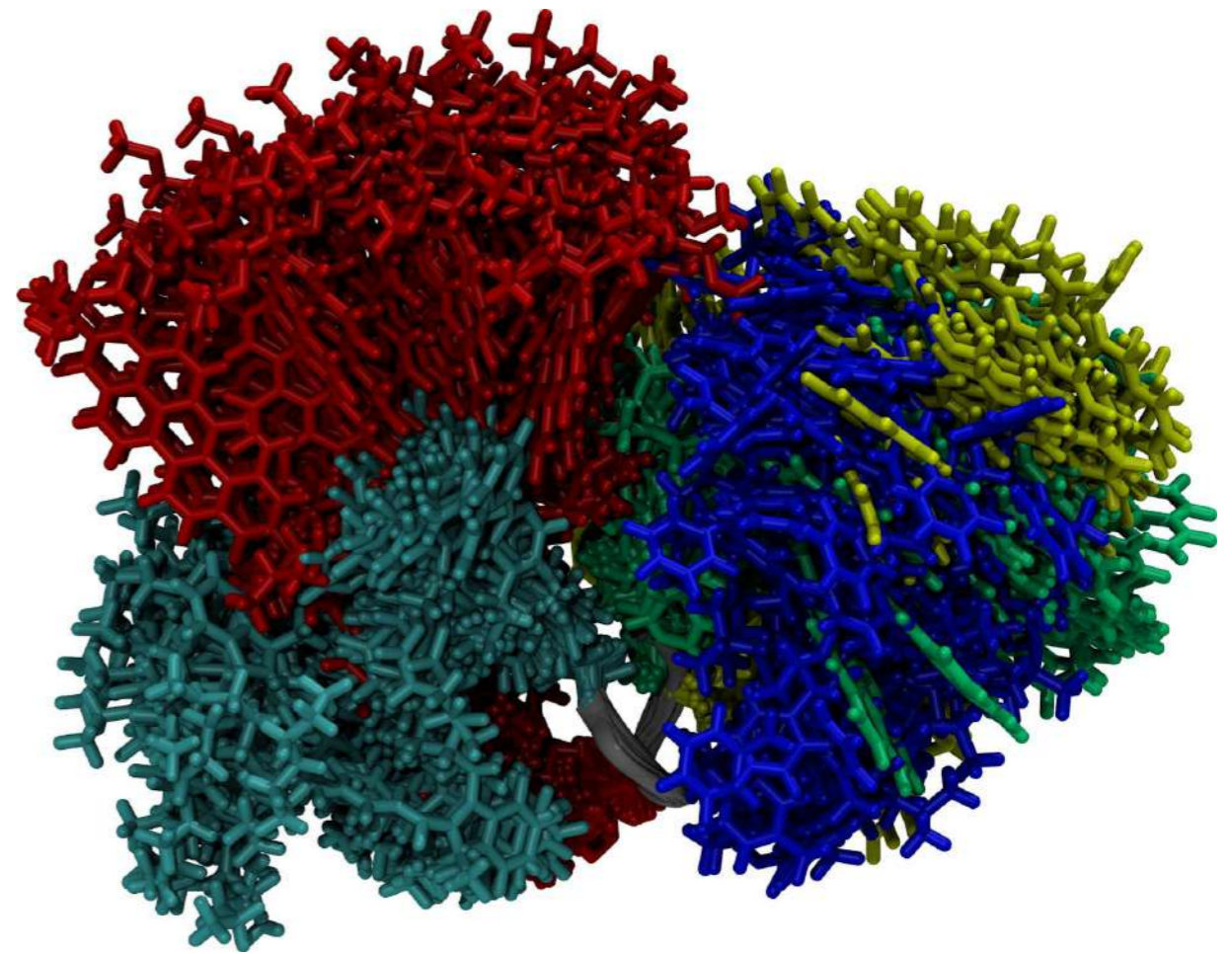
Min2 { within 1.0%  
within 0.5%

Free Energy -245.54 kJ/mol

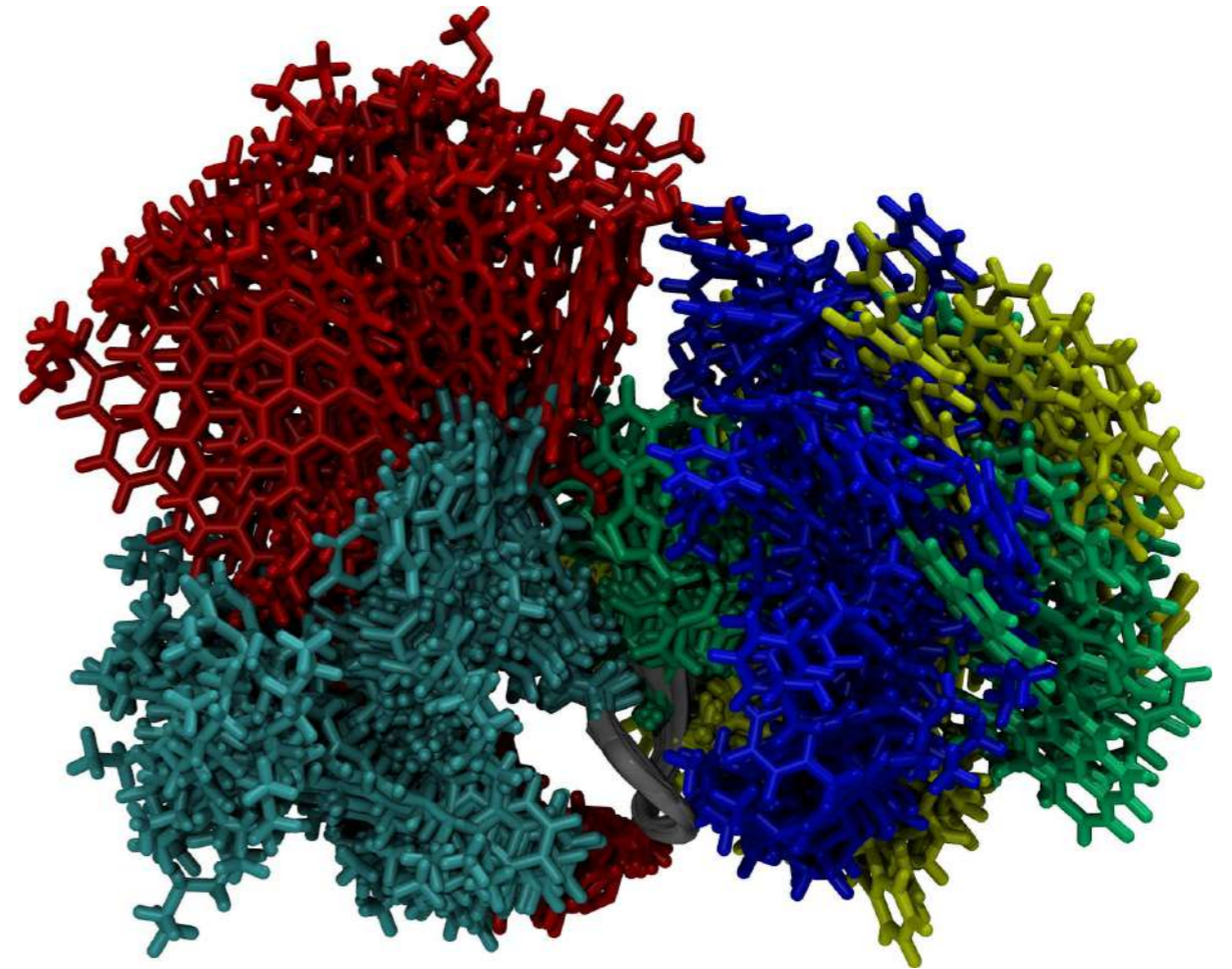
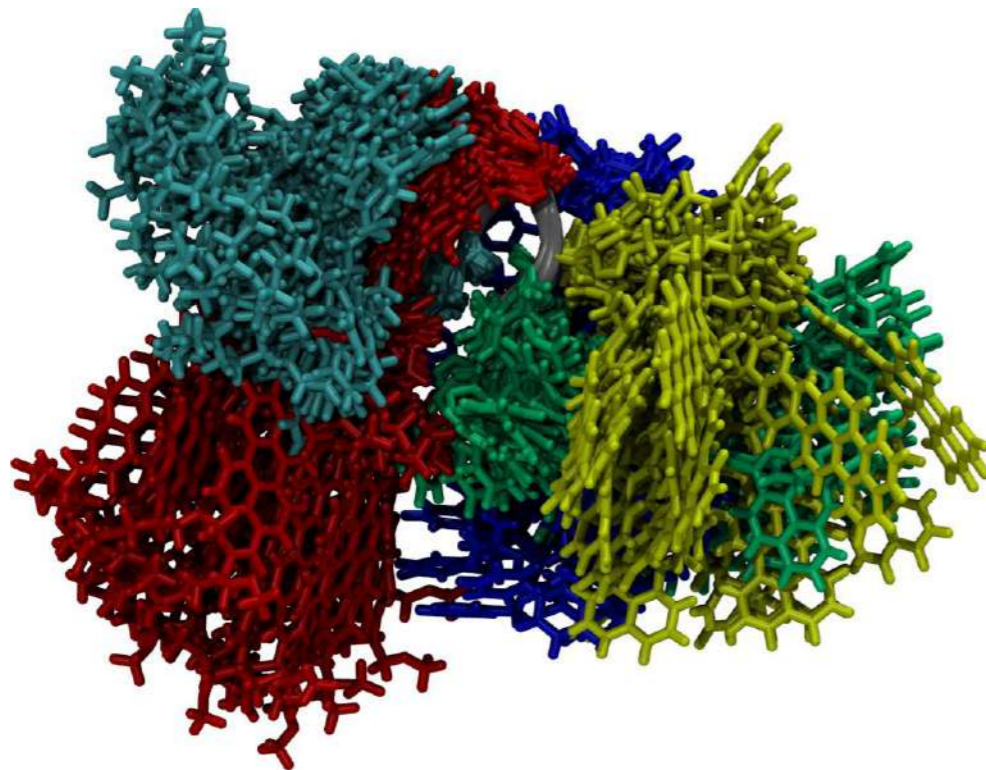
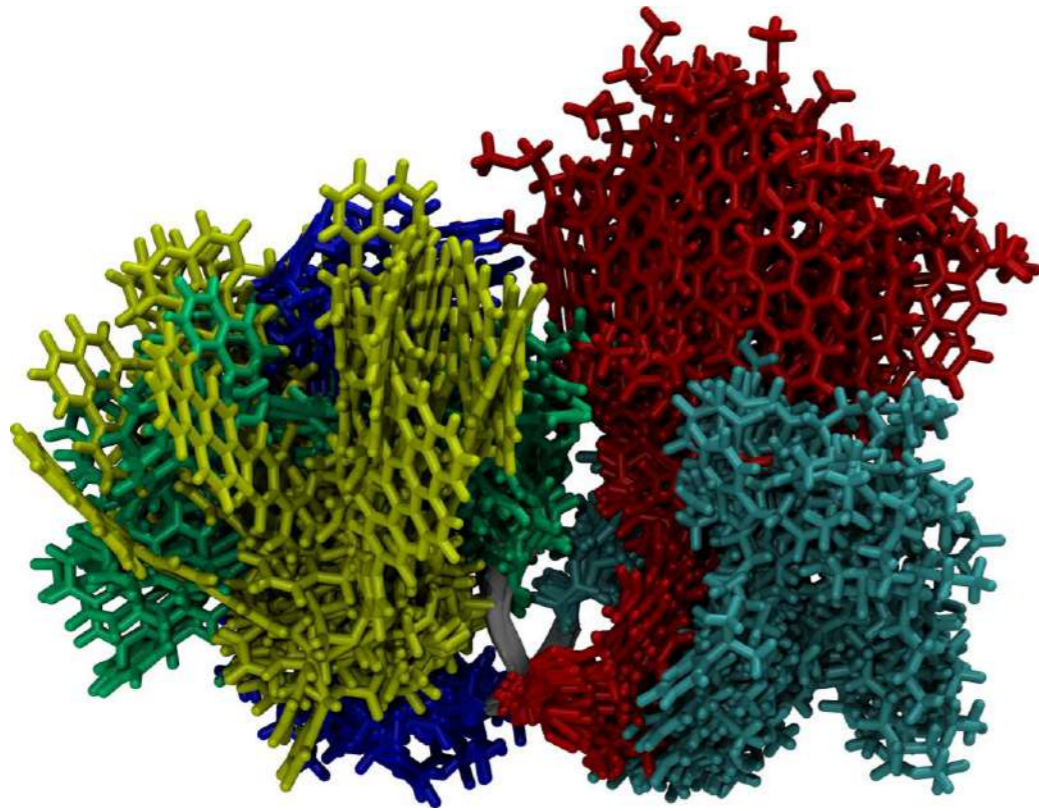
{ A (40%)  
B (60%)



Min1, conf1



Min1, conf0





**TPS 1**

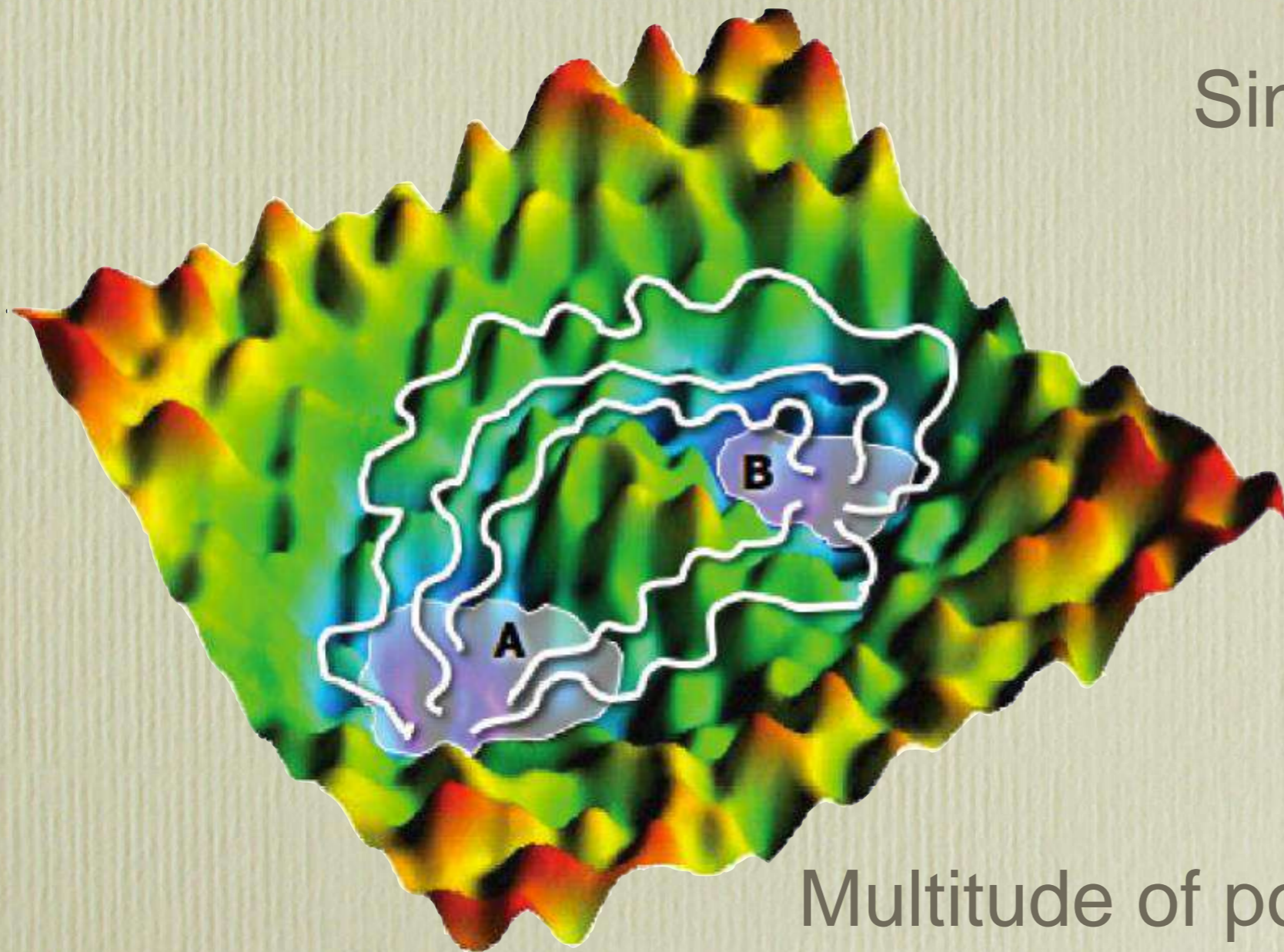
# Details

- Carbon
- DFTB/cp2k C-C
- Graphite → Diamond, then lower T
- shooter, external script
- MD → shooting move → MD → .....

# Corrugated Landscape of Complex Systems

Transition *path*

Single Mechanism →  
saddle point(s)



Multitude of points become relevant,  
only some of them stationary.

Transition *path ensemble*

(D. Chandler, C. Dellago)

```
&FORCE_EVAL
&DFT
&QS
  METHOD DFTB
  &DFTB
    SELF_CONSISTENT F
    ORTHOGONAL_BASIS F
    DO_EWALD F
    &PARAMETER
      PARAM_FILE_PATH .
      SK_FILE C C .././cc
    &END PARAMETER
  &END DFTB
&END QS
&SCF
  SCF_GUESS NONE
  MAX_SCF 1
  &MIXING
    METHOD DIRECT_P_MIXING
    ALPHA 1.
  &END
&END SCF
&END DFT
STRESS_TENSOR DIAGONAL_NUMERICAL
&END FORCE_EVAL
```



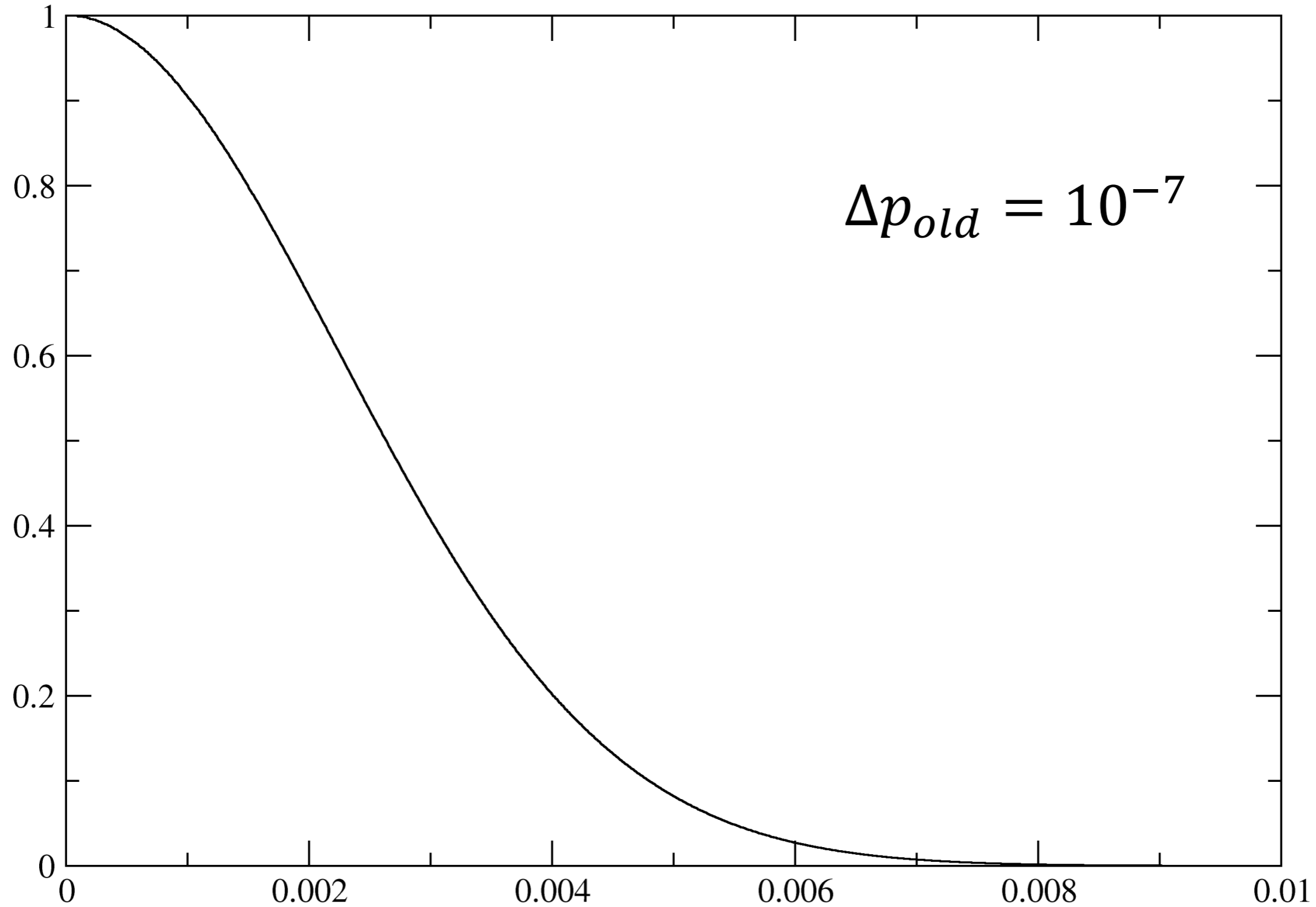
```
&MOTION
&MD
  ENSEMBLE NPT_F
  STEPS xstepsx
  TIMESTEP xtimestepx
  TEMPERATURE 300.0
&THERMOSTAT
  &NOSE
    TIMECON 300
    LENGTH 6
    YOSHIDA 3
    MTS 2
  &END NOSE
&END
&BAROSTAT
  PRESSURE [kbar] 150.0
  TIMECON 50000
&END BAROSTAT
&END MD
&PRINT
&RESTART_HISTORY ON
  &EACH
    MD 1000
  &END
&END
&VELOCITIES ON
  &EACH
    MD 100
  &END
&END
&TRAJECTORY
  &EACH
    MD 10
  &END
&END TRAJECTORY
&CELL LOW
  &EACH
    MD 10
  &END
&END CELL
&RESTART LOW
  &EACH
    MD 1000
  &END
&END RESTART
&END PRINT
&END MOTION
```

# Acceptance Criteria

Shooter

$$\mathcal{P}_{\Delta p_{o \rightarrow n}} \propto e^{\frac{-\Delta p_{shooting}^2}{\Delta p_{old}}}$$

$\mathcal{P}_{\Delta p_{o \rightarrow n}}$



$\Delta p_{old} = 10^{-7}$

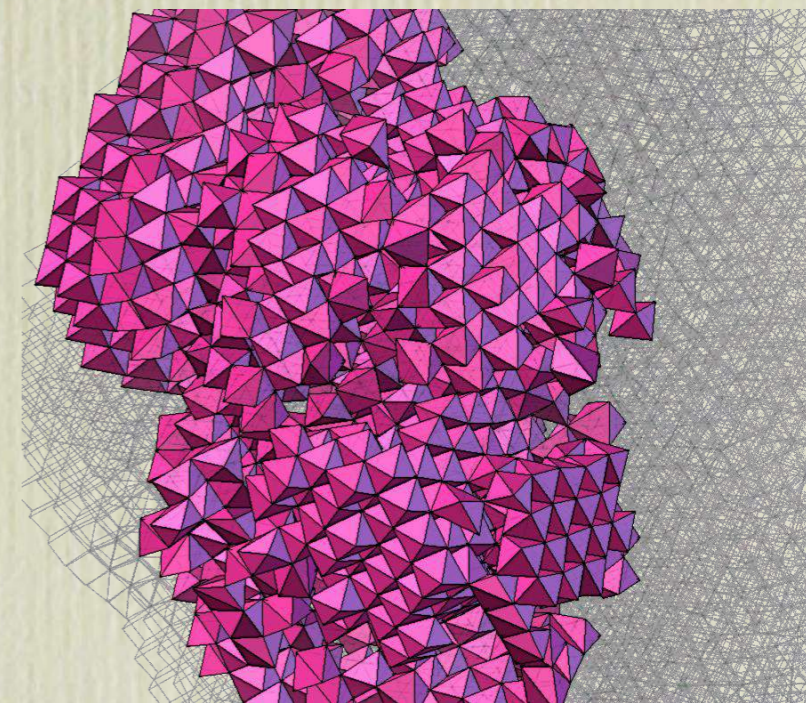
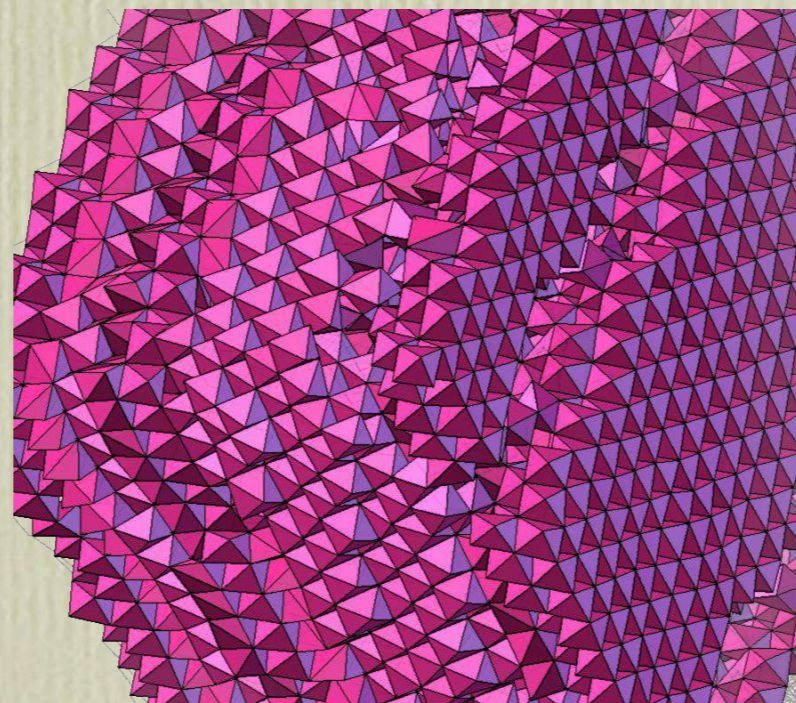
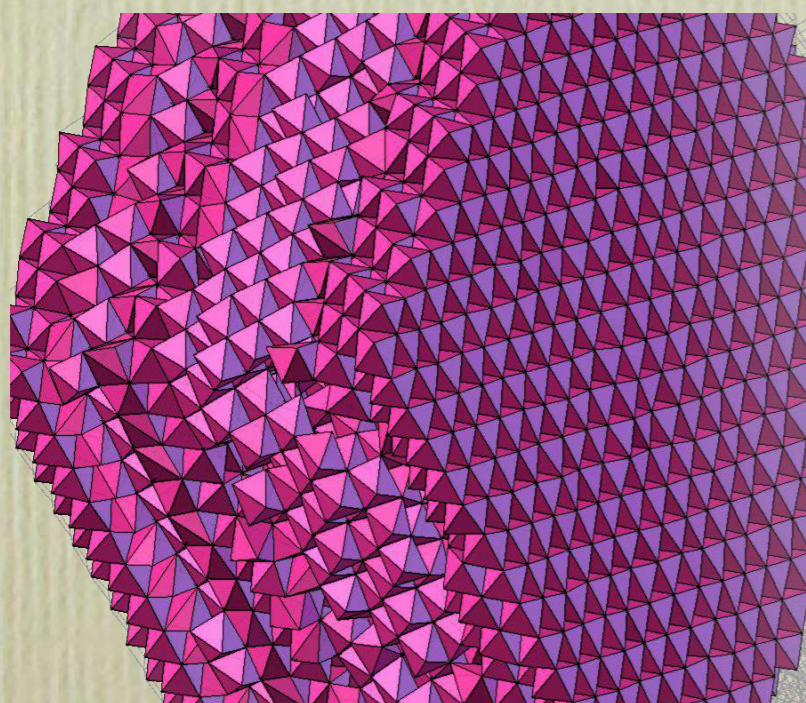
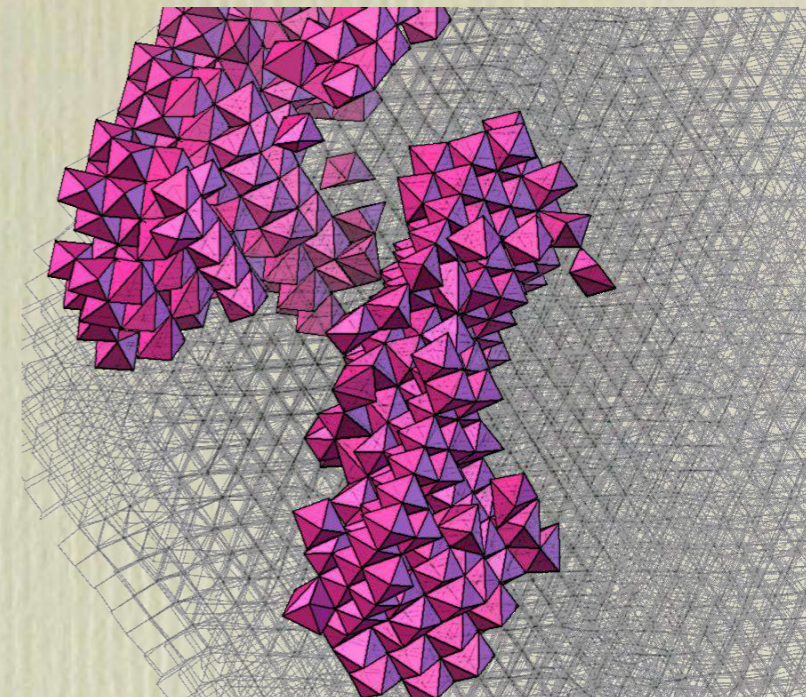
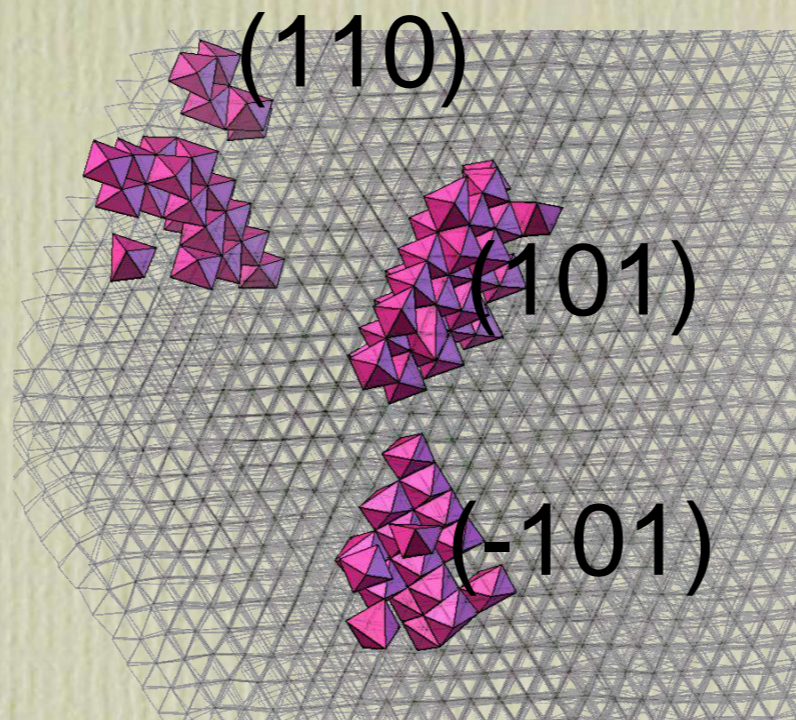
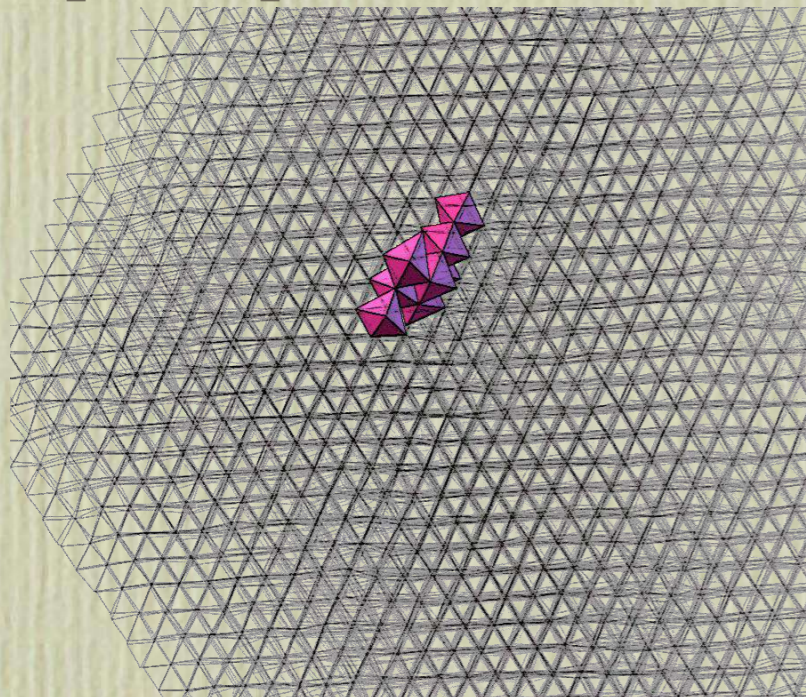
$\Delta p_{shooting}$

# Details

- CdSe
- FF (LJ + partial charges on Cd/Se)
- $W \rightarrow RS$  (model)
- shooter, external script
- MD  $\rightarrow$  shooting move  $\rightarrow$  MD  $\rightarrow$  .....

# Focus on nucleation

[111]



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